

## 3D Building Reconstruction using Linear Edge Segments

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### ABSTRACT

In this article an algorithm aiming on the automatic reconstruction of buildings is described. For this purpose three-dimensional line segments representing roof break-lines are used. Basic idea of the algorithm is to simplify the image interpretation necessary for the building reconstruction by the integration of height data.

### 1. INTRODUCTION

In recent times the acquisition of three-dimensional databases for urban areas has become a topic of growing interest to the photogrammetric community. Simulations that require the representation, management and analysis of three-dimensional descriptions have become standard applications for planning purposes in built-up areas. One example is the propagation of electro-magnetic waves that can be simulated for planning optimal locations of transmitter stations. A similar application is the simulation of the propagation of noise or exhaust fumes near planned roads in built-up areas. Analyzing the impact of new buildings or parks on the micro-climate in urban areas is another topic. A widespread application is the computation of arbitrary perspectives or even animated fly-throughs to visualize urban scenes. Thereby the impression of new buildings within their surrounding can be presented effectively to persons involved in the planning process. The great market for this kind of applications is shown by the fact that architectural offices spend approximately 20% of their budget for the representation of their concepts. Realistic rendering of urban scenes is achieved by techniques like shading the object surfaces due to arbitrary light sources, or by texture mapping to represent different surface materials. If terrestrial images of the building facades are available they can be projected to the building faces. Terms like virtual reality or cyber space stand for the rapid progress and the growing number of applications in this area.

Objects relevant for the description of urban areas are buildings, streets and Digital Terrain Models; this article concentrates on the reconstruction of buildings. The acquisition of the database for urban areas is frequently done by the analysis of aerial imagery since photogrammetric data is three-dimensional, exact, largely complete and up-to-date. Because manual interpretation is very time consuming, a lot of effort has been spent to speed up this process by automatic or semi-automatic procedures. In the short- and middle-term the human visual system will be superior to existing computer vision algorithms in interpreting complex, natural scenes like they occur frequently in aerial images. The idea beyond semi-automatic approaches is to utilize the specific strengths of the human observer and the computer. The interpretation is done by the human operator who e.g. has to select a building model from a library of basic building types and project it into the image. The exact measurement of the building parameters within the image then can be performed automatically. Examples of semi-automatic systems are given in (Quam & Strat 1991) or (Lang & Schickler 1993). Especially in town centers or medieval towns the shape of buildings can be very complex. Still in many regions, like suburbs or industrial areas, buildings can be described by a small number of simple basic types. Within these regions of relatively small complexity, the use of automatic procedures for building reconstruction like the one presented in this article is very promising.

A common technique used by most existing procedures is to utilize linear edge segments as initial primitives. This makes use of the very general knowledge, that buildings consist of a number of straight three-dimensional lines. In the next step rectangular structures which are typical for the presence of buildings in aerial imagery are detected by combining these line segments on relations like

collinearity, parallelism, symmetry and neighborhood. Since this shape model is valid for many man-made objects, like rectangular places, shadows of buildings, or small field parcels, a lot of wrong building hypotheses are detected. In the last step, these building hypotheses have to be verified and 3D descriptions have to be computed by techniques like stereo matching or shadow analysis (Mohan & Nevatia 1992) (McKeown & McGlone 1993). One major problem of the automatic interpretation of images is their great complexity. Images contain a lot of information which is irrelevant for tasks like building reconstruction. Grey-values are influenced by object geometry but also by other factors like illumination (shadows, reflections), surface material and texture. This frequently makes it very hard to separate important information from irrelevant details. In principle a task like building reconstruction can be solved using only aerial images. From a practical point of view height data, containing much geometric information without unnecessary details, can support the solution of this problem considerably. For this reason height and image data are combined in the algorithm for automatic building reconstruction which is described in this article.

To define regions of interest a *building detection* is performed by searching for local maxima in a Digital Elevation Model (DEM). This is based on the knowledge that buildings are objects of limited size rising from the terrain surface. Within these regions a *feature extraction* is performed using DEM data in combination with a stereo image pair. This step aims on the extraction of three-dimensional line segments likely to be roof break-lines (chapter 2). The *building reconstruction* then can be realized by matching the extracted lines against the lines of a building model (chapter 3). Results of the approach are presented (chapter 4), followed by some concluding remarks (chapter 5).

## 2. EXTRACTION OF ROOF BREAK-LINES

Three-dimensional line segments are used by the proposed algorithm for building reconstruction. These lines are extracted from stereo image pairs of known exterior orientation and a Digital Elevation Model. Local maxima in height are searched in the DEM data as a first processing step to focus further computation on regions, where buildings are likely to be present. A detailed description of the performed building detection using DEM data can be found in (Haala 1994). Of course a local maximum in height can be caused by a tree or some other object rising from the terrain surface. Still the detection of these regions can be used effectively to trigger the succeeding geometric building reconstruction. By the elimination of the detected local maxima the topographic terrain surface is computed approximately as further output of this step.

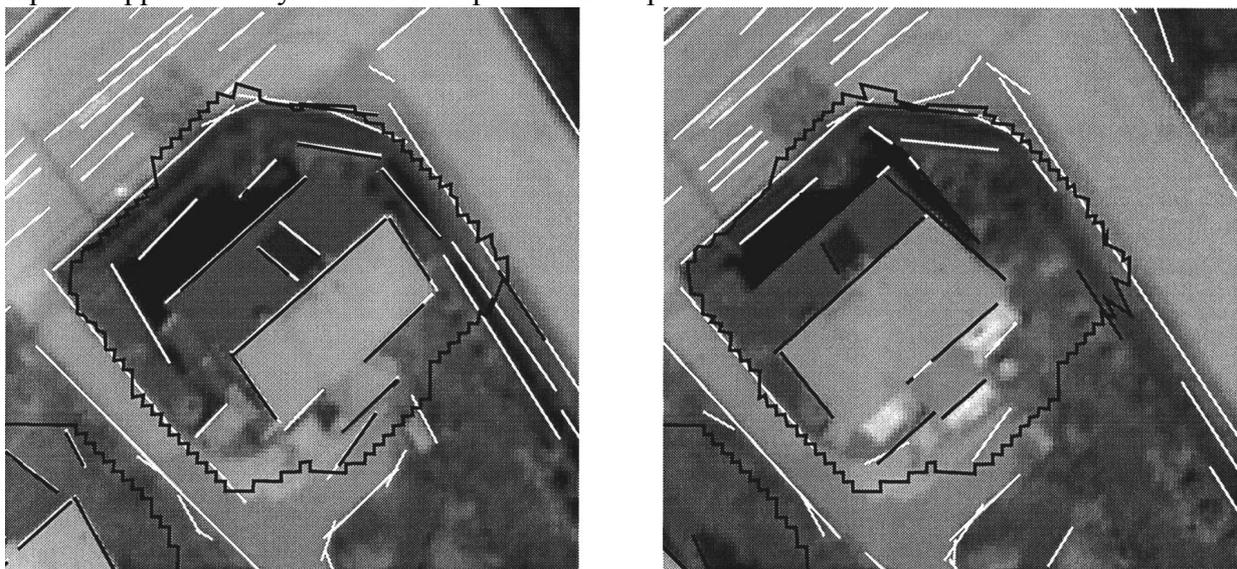


Figure 1: Section of a stereo image pair with extracted grey-value edges (white), detected region of attention (black border line) and selected three-dimensional line segments (black).

One method to acquire three-dimensional linear segments used for building reconstruction is to extract lines from a stereo image pair. Figure 1 presents results of detected regions of interest and the feature extraction, illustrated by a small part of the stereo image pair. Grey-value edges approximated to straight line segments are extracted by an algorithm proposed by Burns, Hansen & Riseman (1986). These lines are superimposed as white lines to the grey-level images. The DEM section shown in figure 2 was used to detect the region of attention which is represented by a black polygon. The black straight line segments are a subset of the white lines. These lines could be determined three-dimensionally by stereo line matching. For this purpose the DEM is used to provide approximate values for the parallaxes of corresponding line pairs. The matching restricts to lines which are located in the region of attention where a building is expected. For the reconstruction only the black 3-D line segments are used.

Image matching techniques like those employed in the program MATCH-T (Ackermann & Krzystek 1991) which was used to provide all height data in this article, show good results in open terrain, but suffer from problems in built-up areas due to occlusions and height discontinuities. Besides factors like image scale and viewpoint, the DEM quality in urban areas mainly depends on the presence of texture at roof regions and the amount of contrast between roof and terrain surface, if image matching techniques are used. This results in considerable differences of DEM quality at roof regions, even in the same image pair. In recent times attempts have been made to improve the results of image matching in urban areas, e.g. using multiple overlapping images or by the integration of potential roof break-lines during the matching process (Maitre & Luo 1992). Due to the independence on the presence of texture, direct DEM measurement by laser scanners is another technique showing very promising results in urban areas (Kilian 1994).

In figure 2 the DEM corresponding to the image section of figure 1 is presented. For this example the building results in a lump within the computed surface. This information is sufficient to detect the building. If the height data is dense and accurate enough, even surface break-lines can be obtained directly from the DEM. Figure 3 shows corresponding sections of a DEM and an image of another data set. For this example the large image scale, the good contrast between roof and terrain surface, and the presence of sufficient texture at roof regions resulted in a very accurate computation of the surface geometry. Therefore the DEM could be used to extract three-dimensional line segments by curvature analysis at convex surface break-lines. These lines extracted from the DEM were projected to the image shown in figure 3.

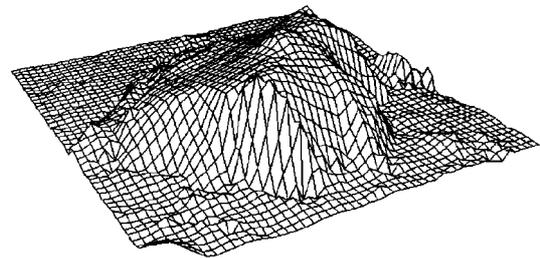


Figure 2: DEM section corresponding to figure 1.

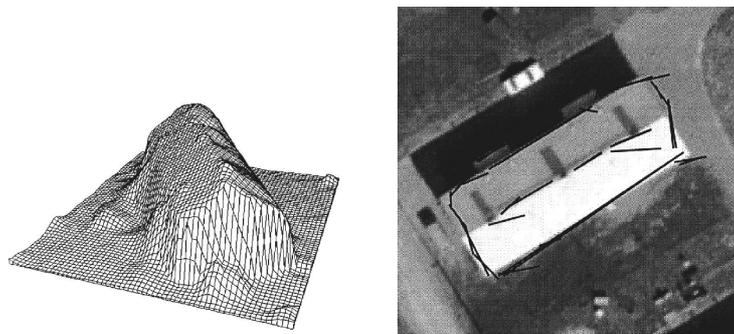


Figure 3: DEM and corresponding image section with extracted DEM break-lines.

### 3. RECONSTRUCTION

Recognition and reconstruction presumes knowledge about the perceived objects. This knowledge is represented by object models. Since we are interested in reconstructing the building geometry, the required model has to represent the shape of the buildings. Reconstruction implies matching primitives which were extracted from the observed data against primitives of the object model. For this reason correspondences between the extracted three-dimensional line segments and the lines of the building model have to be found. These correspondences then can be used to reconstruct the shape of the observed buildings.

#### 3.1 Parametric building model

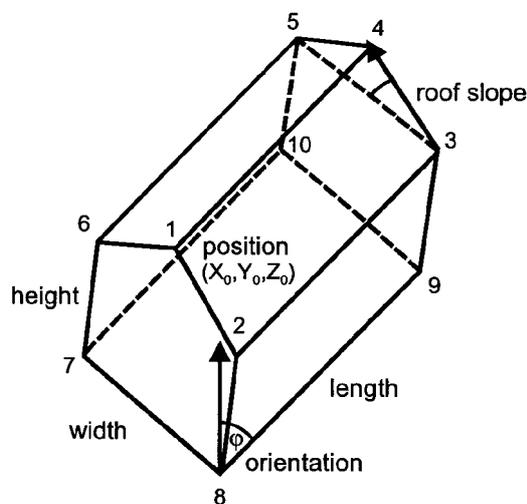


Figure 4: Parametric model of a rectangular building with saddle roof.

Many applications where three-dimensional descriptions of buildings are used do not demand too much detail. To compute realistic simulations or visualizations not each chimney, bay or ledge has to be represented. For this reason the shape of many buildings can be described sufficiently by a few basic models. A common way to describe objects of fairly simple shape is to use parametric models. By this kind of model, objects of the same type are represented by a fixed set of parameters. The individual objects only differ in the parameter values. The shape of the used type of building which is shown in figure 4, can be described by the *length* and *width* of the building, the *slope* of the roof, and the *height* between the roof eaves and the terrain surface. The *position* of the building within the geographic coordinates system is defined by the  $X_0, Y_0, Z_0$  coordinates of a selected point, the *orientation* of the building is defined by the orientation  $\nu$  of the ridge line. To

determine these parameter values for observed buildings, the lines of this building model have to be matched against extracted three-dimensional line segments.

At the moment only rectangular buildings with saddle roof are reconstructed by the proposed algorithm. Even though other models, like those shown in figure 5 will have to be added, this single model is sufficient to reconstruct a considerable portion of buildings.

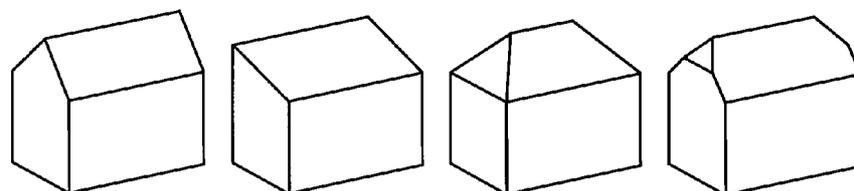


Figure 5: Rectangular buildings with different roof shapes.

#### 3.2 Matching

Due to perspective, projection and occlusion, vertical walls of buildings in general are not visible in an aerial image. Despite from occlusion by other objects like trees or larger buildings this is not a problem for the roof of a building. Therefore, the linear 3-D segments, extracted in the preceding steps, are used

to reconstruct the roof of the building. The height of the building can be determined in a second step by computing the differences between the eaves and terrain heights.

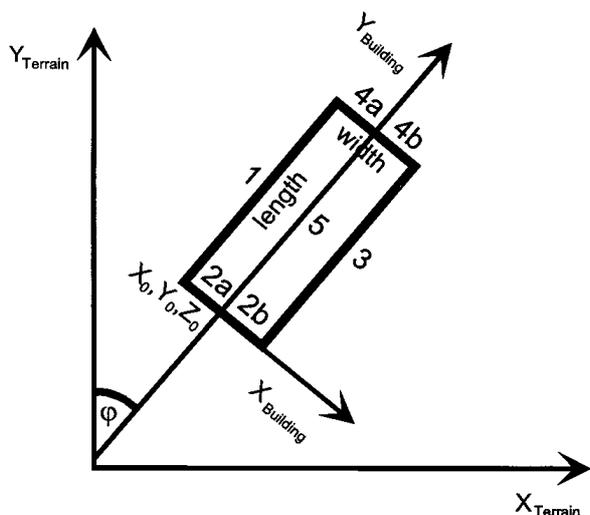


Figure 6: Different types of roof-lines.



Figure 7: Part of the ortho image, extracted line segments (black) and detected groupings (white).

Aiming on object reconstruction, correspondences between the observed primitives and the object primitives have to be found, i.e. the extracted line segments have to be matched against corresponding lines of the roof model. The used model consists of 5 different types of roof lines. These lines are labeled by the numbers 1 to 5 in figure 6. A roof can be reconstructed by extracted line segments, if correspondences are defined for both gable lines (labels 2 and 4) and for two of the roof lines parallel to the ridge (labels 1, 3 and 5). In that case the group of matched lines is arranged rectangular. Therefore groups of lines, that can be used to reconstruct a roof, are detected by searching for rectangular combinations of the extracted three-dimensional line segments. These structures can be detected by a process which combines four lines respectively, applying relations like proximity, parallelism and right angles.

Figure 7 shows the detected rectangles and the used linear segments projected into the ortho image. The slope and relative height of the four grouped linear segments are essential features for establishing correspondences between model lines and observed lines. One pair of opposite lines of the four grouped lines is parallel to the ground plane. If both lines are of the same height, they define the eaves of the roof (labels 1 and 3), if one of these two lines is higher than the other then this line defines the ridge of the roof (label 5). The second pair fits to the front sides of the building and defines gable lines of the roof (labels 2 and 4). The example presented in figure 7 shows several grouping results in which lines representing break-lines of the roof are involved as well as texture and shadow lines. Mismatched lines are another reason for the multiple overlapping rectangles constructed by the grouping. Because a lot of wrong correspondences are defined which have to be rejected, the detected groupings have to be evaluated in a further step.

### 3.3 Estimation of roof parameters

The matching results in possible correspondences between extracted lines and model lines. To evaluate these matching hypotheses, i.e. to decide whether the four combined lines really fit to the used roof model, a least squares adjustment is performed. Within this step the parameters ( $X_0$ ,  $Y_0$ ,  $Z_0$ ,  $v$ , *length*, *width* and *slope*) are estimated by minimizing the distances between the observed linear segments and

the corresponding model lines, i.e. the shape and position of the roof is determined. The error of the residual sum of squares of the least squares adjustment measures the overall discrepancy between the observed lines and the fitted roof model. This measure is used to accept or reject a reconstruction, i.e. the matching can be verified.

Residuals are defined by the endpoints of the matched three-dimensional line segments. An example of a line segment, corresponding to an eaves line of the roof (label 1) is given by the following equations.

$$X_{\text{Building}} + \text{width}/2 =$$

$$\cos \nu \cdot (X_{\text{Terrain}} - X_0) - \sin \nu \cdot (Y_{\text{Terrain}} - Y_0) + \text{width}/2 = r_i \quad (1)$$

$$Z_{\text{Terrain}} - Z_0 = r_j \quad (2)$$

The perpendicular distance of the point  $P_{\text{Terrain}}$  to the corresponding model line is split into a part parallel to the ground plane, defining the residual  $r_i$  and a part in the direction of the Z-axis which defines the residual  $r_j$ . The other matched lines are treated in a similar way, so the four grouped lines result in 16 observations which are used to estimate the 7 parameters of a roof. If a combination of lines results in a small error and is accepted for this reason, further lines are included in the estimation process. Therefor extracted line segments are matched against proximate lines of the reconstructed building. Finally the reconstruction with the smallest error  $\sigma_0$  is selected for each detected region of interest.

#### 4. RESULTS

To demonstrate the capabilities of the proposed approach it was applied to the ISPRS WG 3 test data sets (Fritsch, Sester & Schenk 1994). Figure 8 shows the left stereo image of a suburban test area, including all reconstructed buildings and the lines used for the parameter estimation. Figure 9 shows a perspective view of that area, computed by projecting image data to the terrain surface. This terrain surface was generated by eliminating the detected local height maxima from the original DEM data; it was also used to compute the height of the building which is defined by the difference between the eaves of the reconstructed roof and the terrain. A building can be reconstructed by the proposed algorithm, if correspondences were found for at least four different lines of the roof model. The reconstruction fails, if one side of a building is completely missing, e.g. due to occlusion by an object like a tree or due to very low contrast in one of the stereo images. This is the reason why 20% of the houses could not be reconstructed in the suburban data set presented in figure 8. The accuracy of straight lines extracted from digital images usually is in the order of 0.3 pixel, corresponding to 10 cm on the terrain surface for the used data sets. In principle, this is the limiting factor for the accuracy which can be achieved by the building reconstruction. This number could be confirmed by the differences between the reconstructed roof corners and points measured manually in the stereo image pair. Of course this is only true, if the shape of the reconstructed building really can be described by the used model. Other reasons for discrepancies between a real building and its extracted description are additional object parts like out-buildings or bays which are not contained in the model and therefore can not be reconstructed.



Figure 8: Left image with reconstructed buildings and used linear segments.

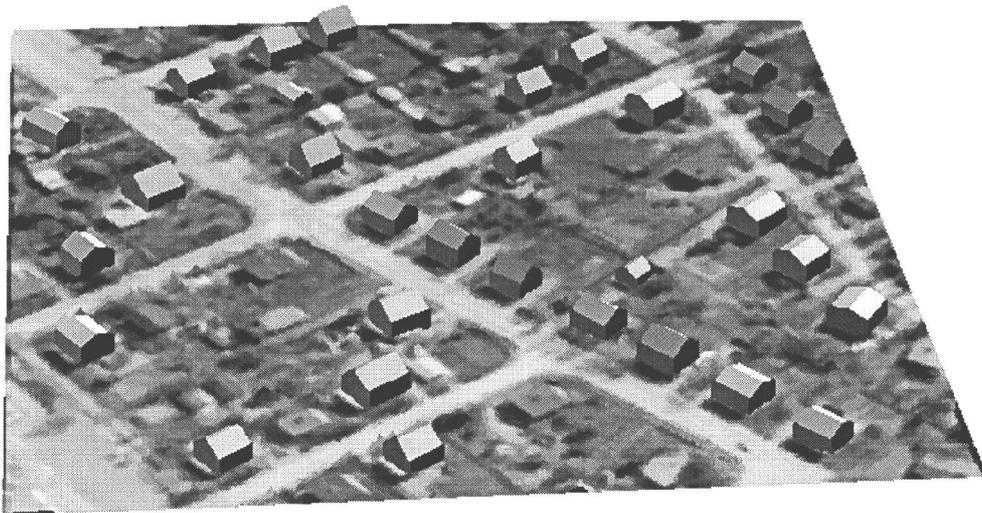


Figure 9: Perspective view of reconstructed 3-D urban model.

In chapter 2 the extraction of potential roof break-lines from stereo images or, alternatively, from DEM data was described. Figure 2 in this chapter shows a typical section of the height data available for the suburban test area which is presented in figure 8. Due to the small size of the buildings and the absence of sufficient texture at roof regions, the quality of the height data for this area is quite poor. Therefore it could only be used to detect regions of interest by searching for local maxima; the reconstruction of the buildings was performed using line segments which were determined by stereo matching of extracted grey-value edges. The second test data set which is presented in figure 10, shows a group of

larger buildings. In chapter 2 an example of the height data available for this region is given in the left image of figure 3. For this data set the good quality of the height data allowed a direct extraction of surface break-lines. Even though extracted image lines would also be sufficient for reconstruction, surface break-lines were used to demonstrate their potential. Figure 10 shows the reconstructed buildings and the used DEM break-lines. For this data set one building could not be reconstructed since the extraction of roof break-lines failed due to the poor DEM quality within this region.



Figure 10: Reconstruction using extracted DEM break-lines.

Grey-value edges are not only caused by surface break-lines or object borders, but also by shadows, reflections or texture. Additionally, a lot of arbitrary lines occur due to mismatching, especially if the height data used to provide approximate parallax is of poor quality. For these reasons frequently three-dimensional line segments are generated which are no roof break-lines. Since all these lines have to be grouped, matched against model lines, and finally rejected, the building reconstruction using this type of lines can be quite time consuming. Lines extracted from the DEM actually are surface break-lines and therefore are more likely to be roof break-lines. On the other hand these lines have less geometric accuracy due to the lower point density of the original data compared to images. Surface break-lines are maxima in the second derivative of the original DEM data, grey-value edges are maxima of the first derivative of the original image data. Since derivation enlarges the effects of noise, this is another reason for line segments extracted from a DEM being less accurate. To utilize the benefits of both data sources the building reconstruction can initially be performed by the DEM break-lines which are more likely to be roof break-lines. In a second step the reconstruction can be refined by the lines extracted from the stereo image pair which are more accurate. A result of this procedure is presented in figures 11 and 12. The initial reconstruction and the used DEM lines are shown in figure 11, the refined reconstruction with the used stereo image lines presented in 12. Other methods of data fusion, e.g. combining DEM lines and image lines during the feature extraction are also possible and will have to be a topic of future interest.



Figure 11: Initial reconstruction using DEM break-lines.



Figure 12: Refined reconstruction using stereo image lines.

## 5. CONCLUSIONS

The integration of image and height data for building reconstruction proved to be very successful, since the object recognition can be simplified considerably compared to pure image interpretation. Height data was mainly used to detect regions of attention, where buildings are expected, but it is also possible to extract the three-dimensional line segments required for reconstruction from the DEM. Up to what extent height data can be used strongly depends on the DEM quality. Techniques like direct measurement of terrain heights by laser scanners are very promising to improve the quality of available height data, so the importance of this kind of data is likely to increase. Integration of other data sources like digital ground plans available for a considerable number of buildings can also be done. Even though this kind of information is very useful for three-dimensional building reconstruction, a major problem that has to be solved is to transform the ground plan into a description which is more suitable for the reconstruction step.

At the moment only one basic type of building is reconstructed by the proposed algorithm. Though in many regions a lot of buildings can be described by the used model, it will be necessary to include some more basic types of buildings. Of course parametric models have their limits, if more complex buildings have to be reconstructed. Therefore the acquisition of more general models which are also able to cope with small modifications of shape, will have to be a topic of future research.

## 6. REFERENCES

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