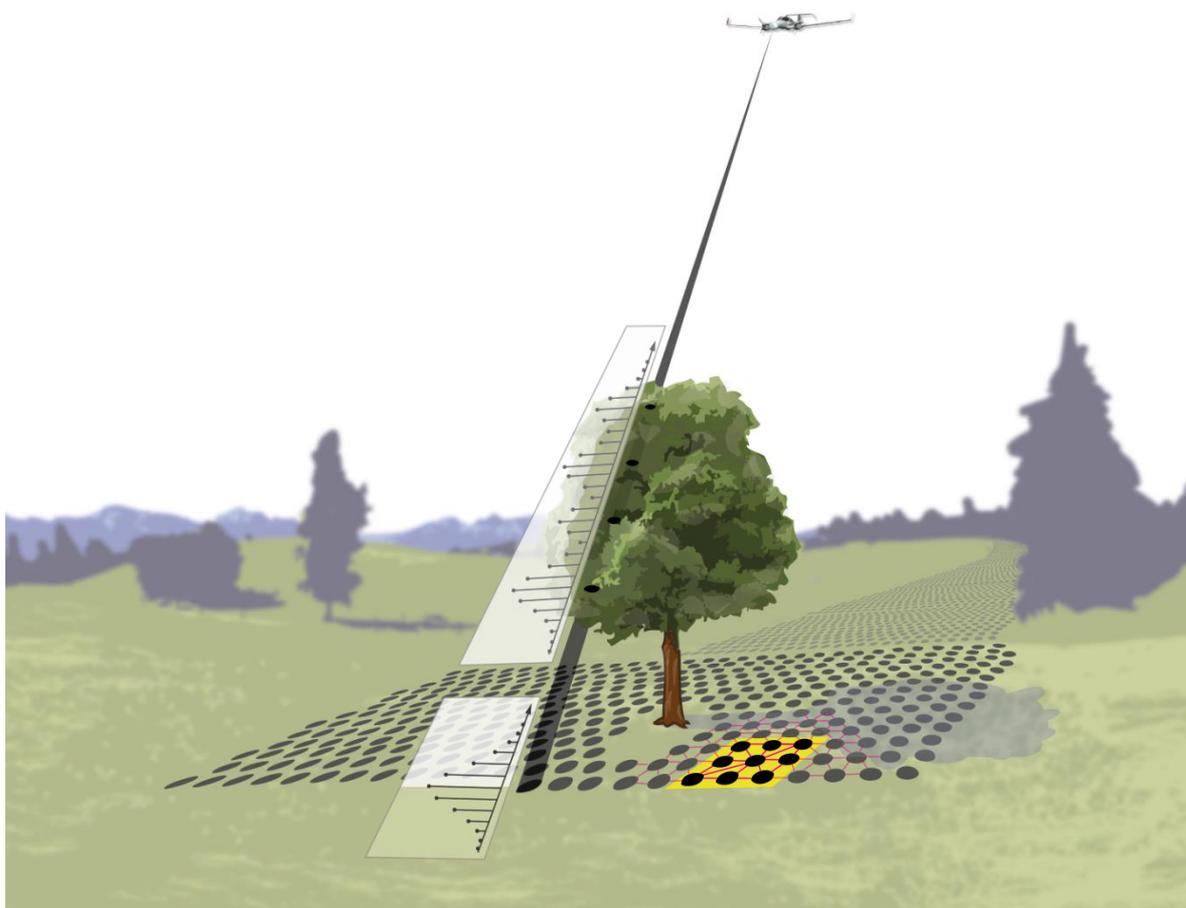




# Sampling the World in 3D by Airborne LIDAR – Assessing the Information Content of LIDAR Point Clouds

**PhoWo 2013**  
September 11<sup>th</sup>, 2013  
Stuttgart, Germany

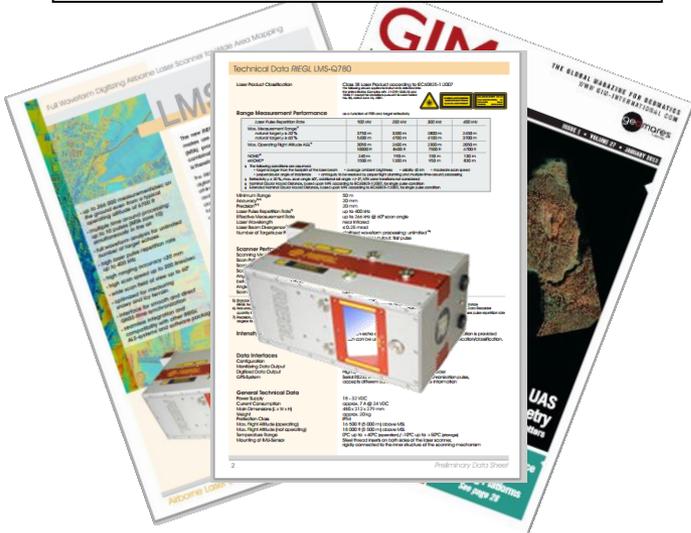
Andreas Ullrich  
*RIEGL LMS GmbH*



- sequential data acquisition
- surface sampling at laser footprints
- “sampling” footprint  $\leftarrow \rightarrow$  single point of point cloud (PC)
- organizing measurements in scan lines
  - intra-line spacing
  - inter-line spacing
- “2D” resolution limited by footprint size
- sampling density impacts information content of PC
- resolution in 3<sup>rd</sup> dimension
- echo-digitization with full waveform analysis  $\rightarrow$  best multi-target resolution



**instrument specification**



density and spacing

LIDAR spec

performance envelope

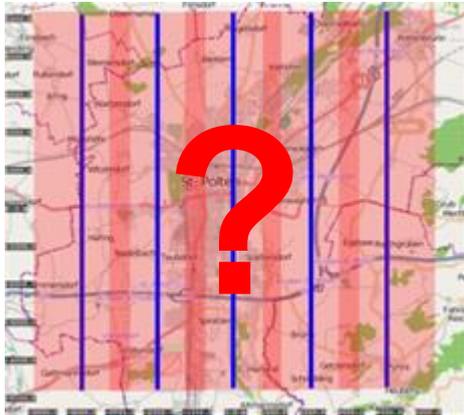
scanner performance

impact of terrain

example on 3D sampling

acquisition time

**How long does the acquisition actually take?**



**What will be the point cloud's sampling quality?**



## LIDAR density and spacing specification

(ASPRS Version 1.0, Draft 2)

LDSS point spacing	LDSS point density
1-dimensional metric	2-dimensional metric
point-to-point distance	points in a given area
unit: meters (feet, yards, cm ...)	unit: points per m <sup>2</sup> (ft <sup>2</sup> , ...)

## LIDAR Guidelines and Base Specification

→ Nominal Point Spacing (NPS)

( U.S. Geological Survey, National Geospatial Program, Version 13)

spatial sampling frequency	point density
1-dimensional metric	2-dimensional metric
inverse of point spacing (1/NPS)	average points in a given area
unit: points per meters (feet, yards, ...)	unit: points per m <sup>2</sup> (ft <sup>2</sup> , ...)



# LIDAR density and spacing specification (ASPRS Version 1.0, Draft 2)

## Unbiased LiDAR Data Measurement (Draft)

Ty Naus, Fugro Horizons, Inc.

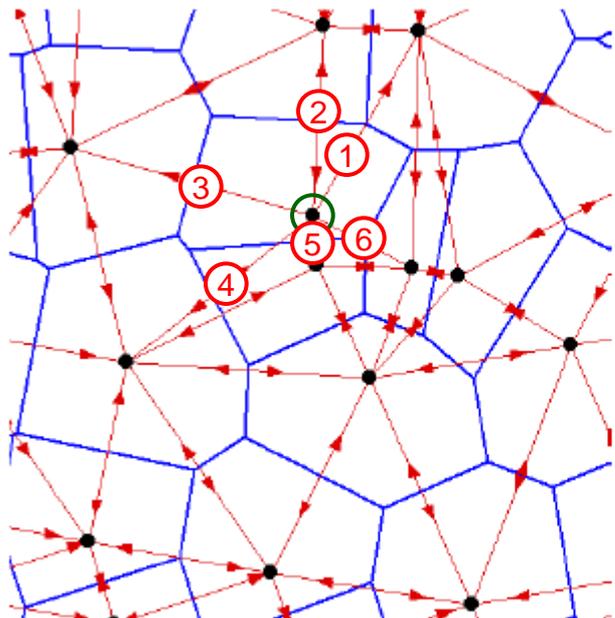
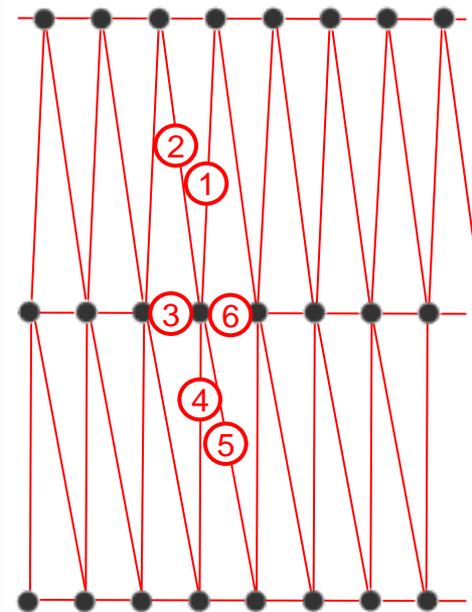


Figure 7b: Voronoi polygons shown in blue for actual LiDAR point distributions – the triangulation edges are shown in red.

$$d_{p-p} = \frac{1}{N} \sum_{i=1}^N d_i$$

average or maximum?



$$d_{p-p} = \max(d_i)$$



	Instrument A	Instrument B	Instrument C
scan mechanism	rotating polygon	oscillating mirror	oscillating mirror
number of channels	single channel	dual laser output	dual laser output
flight altitude, AGL <sup>1)</sup>	50 m - 3500 m	150 m - 3500 m	150 m – 5000 m
laser pulse rate	100 kHz - 400 kHz	2 x 40 kHz – 2 x 250 kHz	2 x 50 kHz – 2 x 250 kHz
measurement rate	66 kHz - 266 kHz	80 kHz - 500 kHz	100 kHz - 500 kHz
pulses in the air	up to 12	2 x up to 2	not disclosed
field of view	0 deg - 60 deg	0 deg - 75 deg	0 deg - 75 deg
scan rate	10 LPS – 200 LPS	0 LPS- 2 x 200 LPS	0 LPS- 2 x 280 LPS

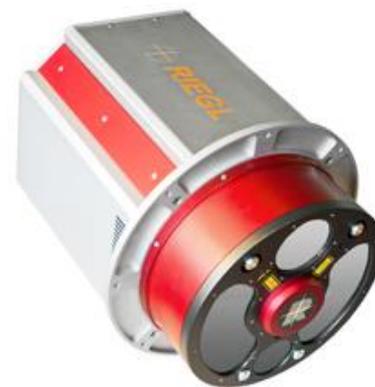


	Instrument A	Instrument A2
scan mechanism	rotating polygon	rotating polygon
number of channels	single channel	dual channel
flight altitude, AGL <sup>1)</sup>	50 m - 3500 m	50 m – 3500 m
laser pulse rate	100 kHz - 400 kHz	2 x 100 kHz – 2 x 400 kHz
measurement rate	66 kHz - 266 kHz	123 kHz – 532 kHz
pulses in the air	up to 12	2 x up to 12
field of view	0 deg - 60 deg	0 deg – 60 deg
scan rate	10 LPS – 200 LPS	2 x 10 LPS- 2 x 200 LPS

**Instrument A**  
**RIEGL LMS-Q780**



**Instrument A2**  
**RIEGL LMS-Q1560**





instrument A

instrument A2

instrument B

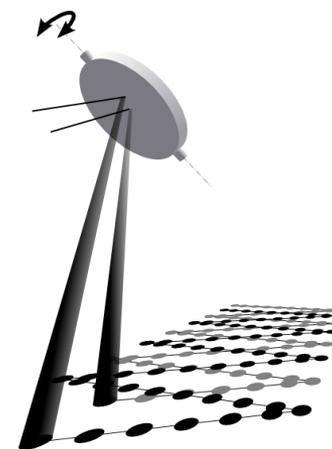
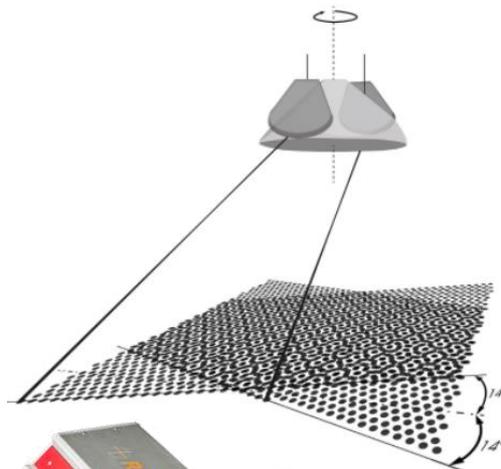
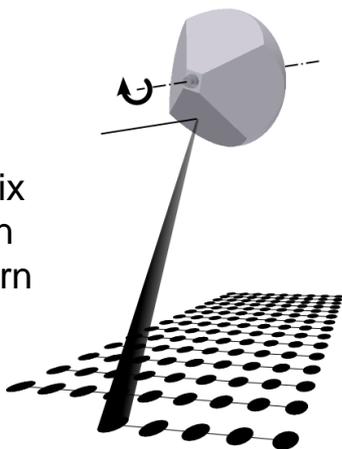
instrument C

rotating polygon,  
single channel

rotating polygon,  
dual channel

oscillating mirror,  
dual laser output

matrix  
scan  
pattern



**RIEGL LMS-Q780**



**RIEGL LMS-Q1560**



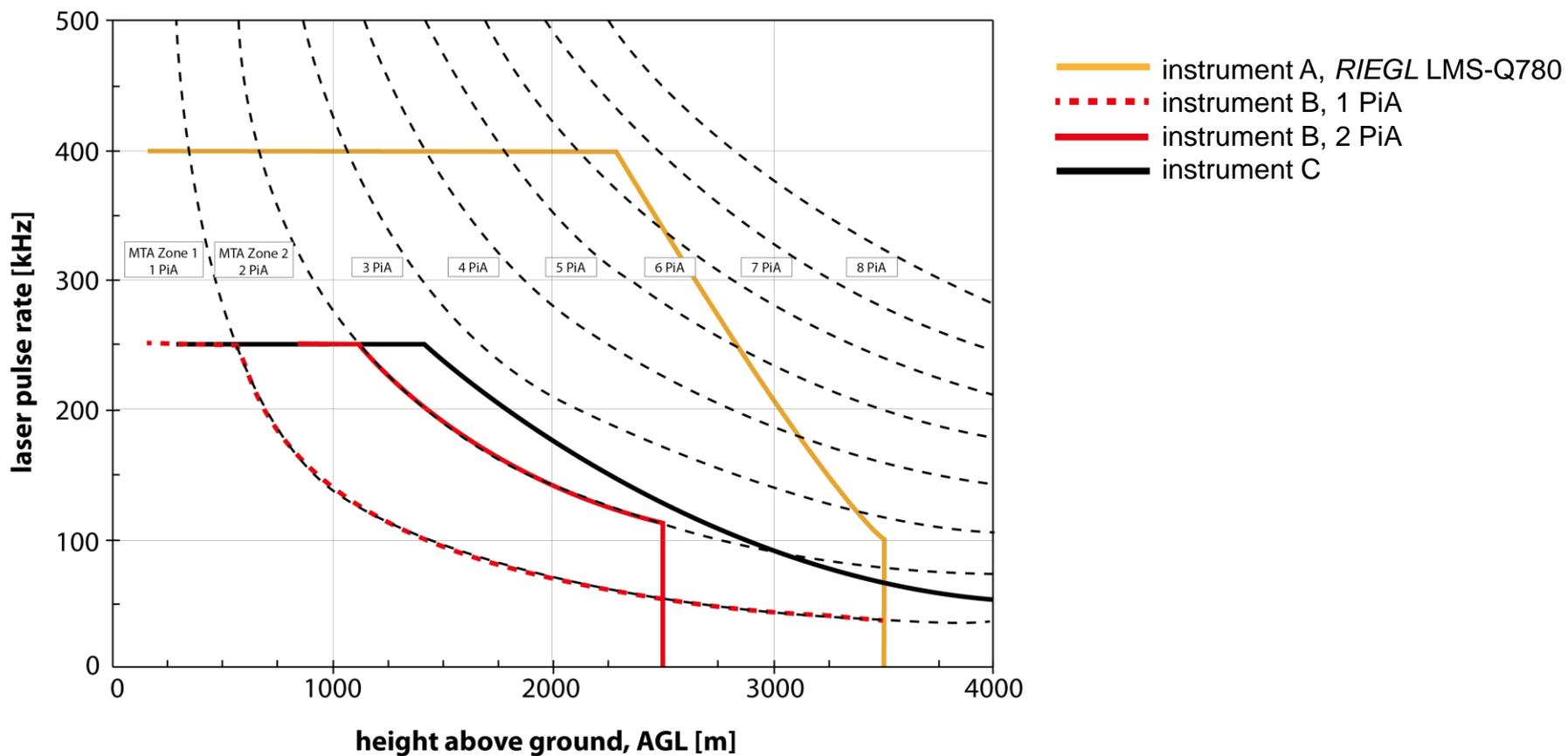
	Instrument A	Instrument B	Instrument C
scan mechanism	rotating polygon	oscillating mirror	oscillating mirror
number of channels	single channel	dual laser output	dual laser output
flight altitude, AGL <sup>1)</sup>	50 m - 3500 m	150 m - 3500 m	150 m - 5000 m
laser pulse rate	100 kHz - 100 kHz	50 kHz - 100 kHz - 2 x 250 kHz	50 kHz - 2 x 250 kHz
measurement rate	66 kHz - 266 kHz	80 kHz - 500 kHz	100 kHz - 500 kHz
pulses in the air	up to 12	2 x up to 2	not disclosed
field of view	0 deg - 60 deg	0 deg - 75 deg	0 deg - 75 deg
scan rate	10 LPS - 200 LPS	0 LPS - 2 x 200 LPS	0 LPS - 2 x 280 LPS

**performance envelope**

**scan speed vs FOV**

<sup>1)</sup> 10% reflectance, 90% detection probability, 40 deg FOV, 23 km visibility

FOV .. field of view, AGL .. above ground level, LPS... lines per second

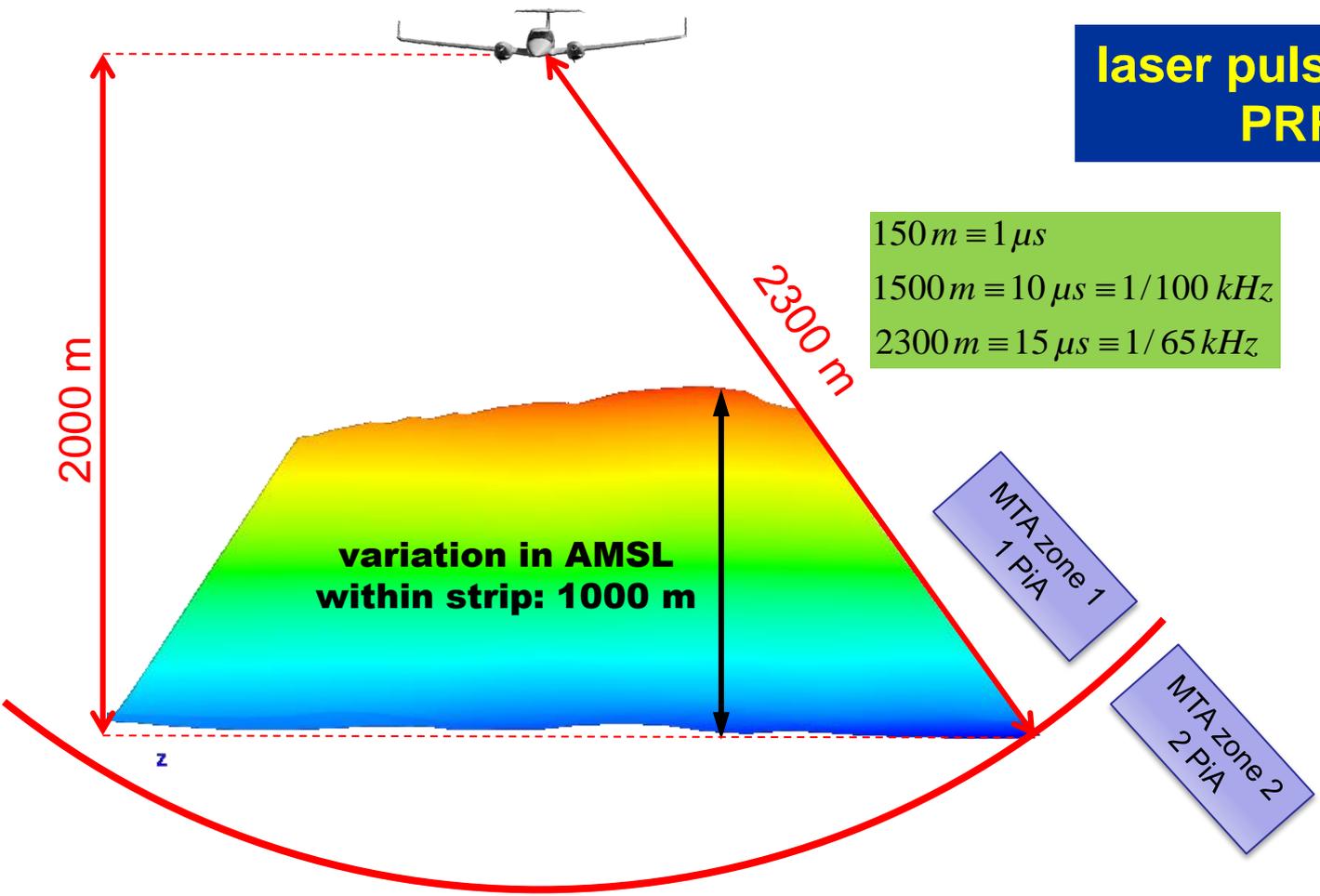
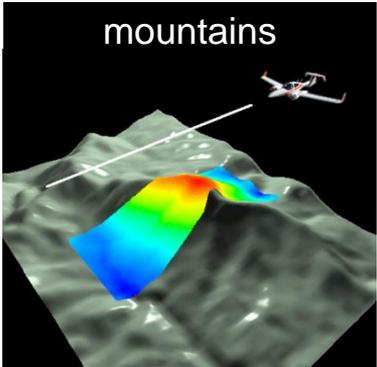


1) 10% reflectance, 90% detection probability, 40 deg FOV, 23 km visibility



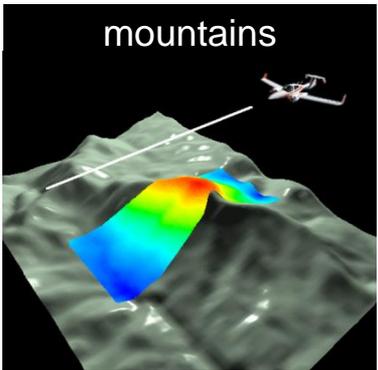
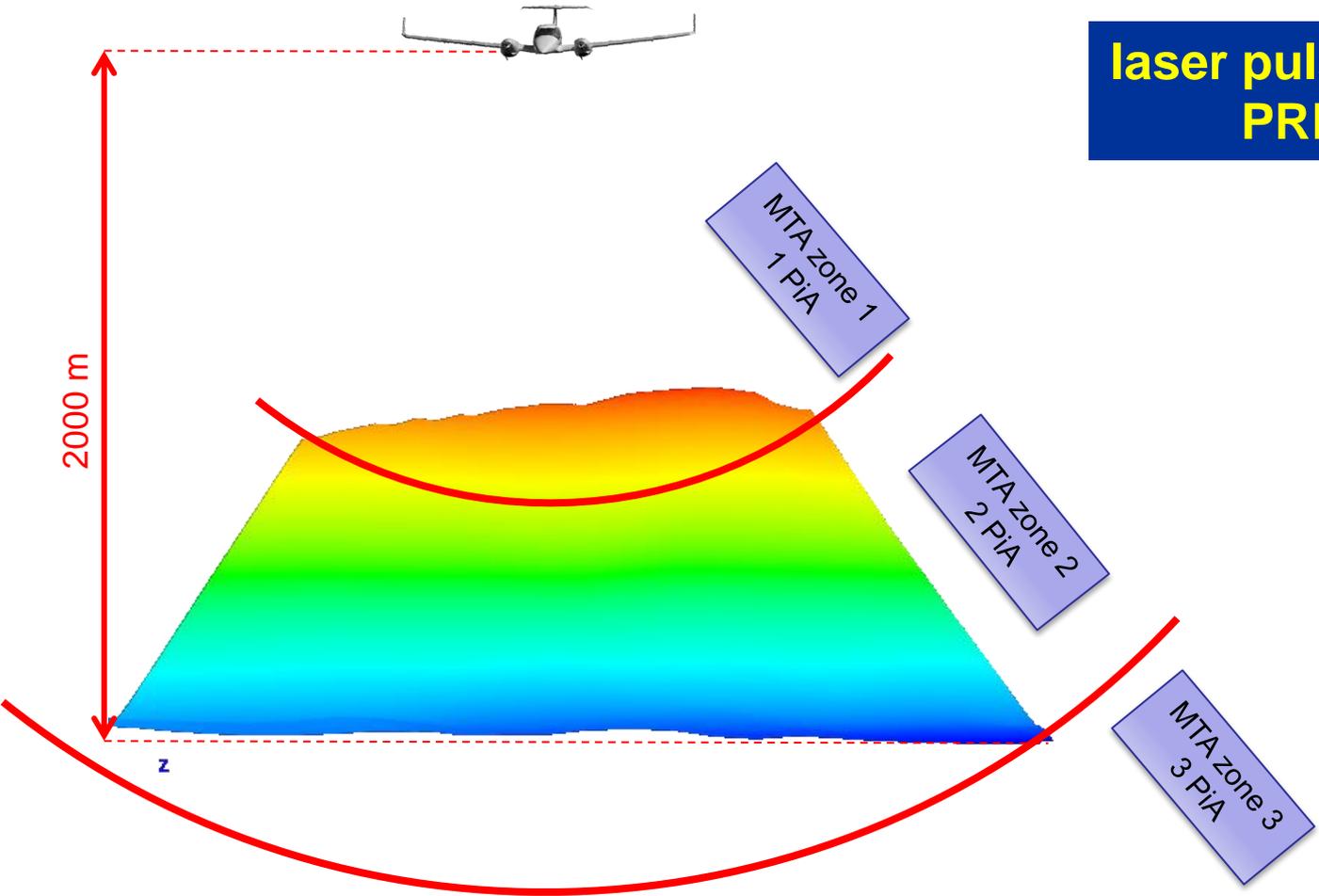
**laser pulse repetition rate  
PRR = 65 kHz**

150 m  $\equiv$  1  $\mu$ s  
 1500 m  $\equiv$  10  $\mu$ s  $\equiv$  1/100 kHz  
 2300 m  $\equiv$  15  $\mu$ s  $\equiv$  1/65 kHz



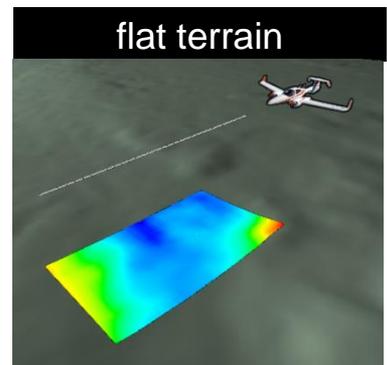
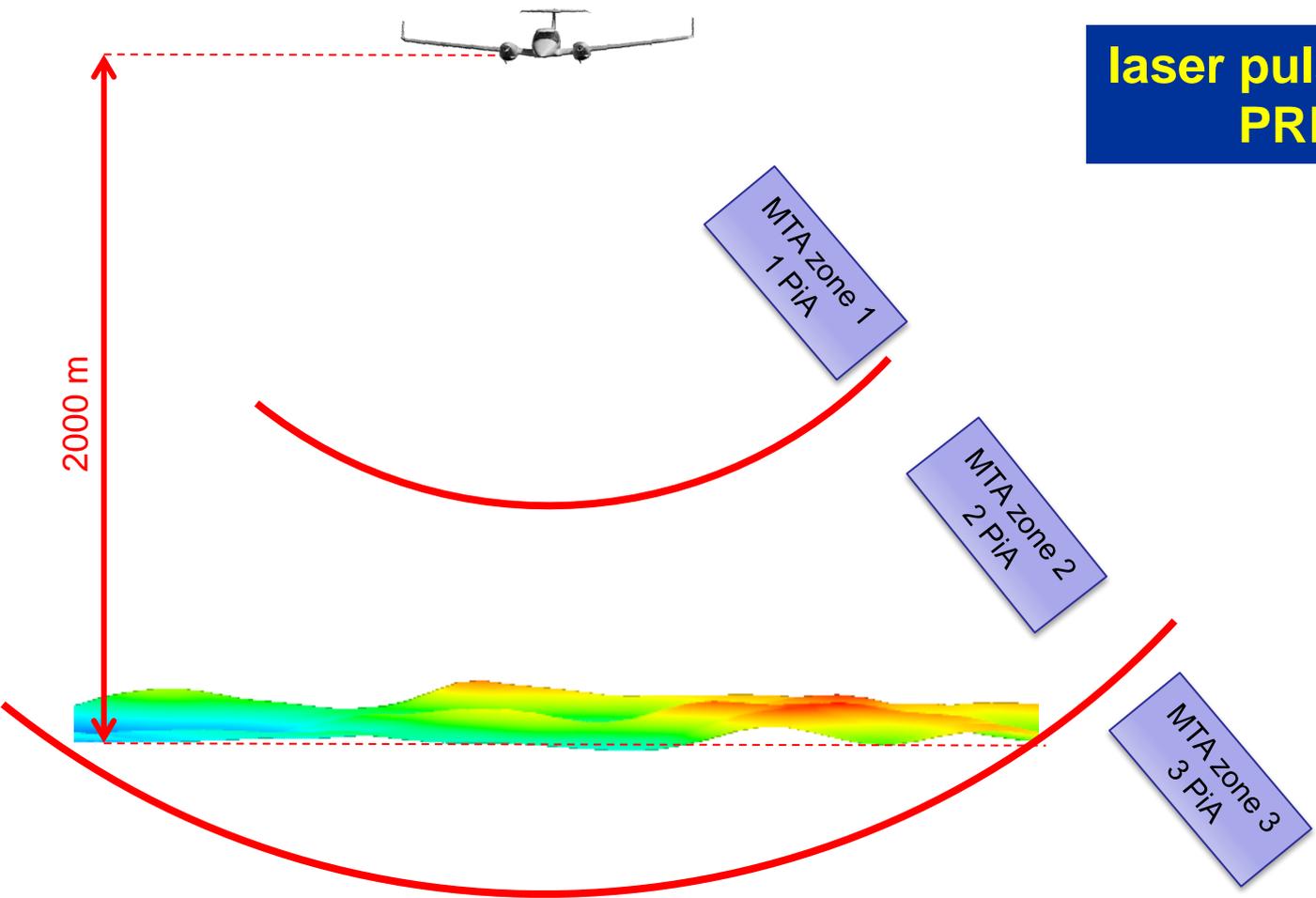


**laser pulse repetition rate  
PRR = 130 kHz**



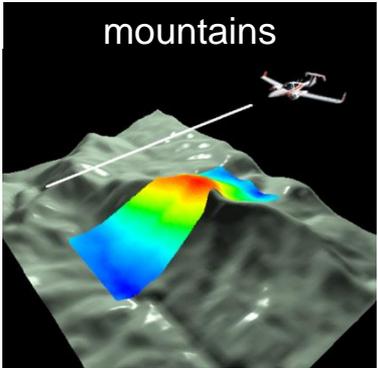
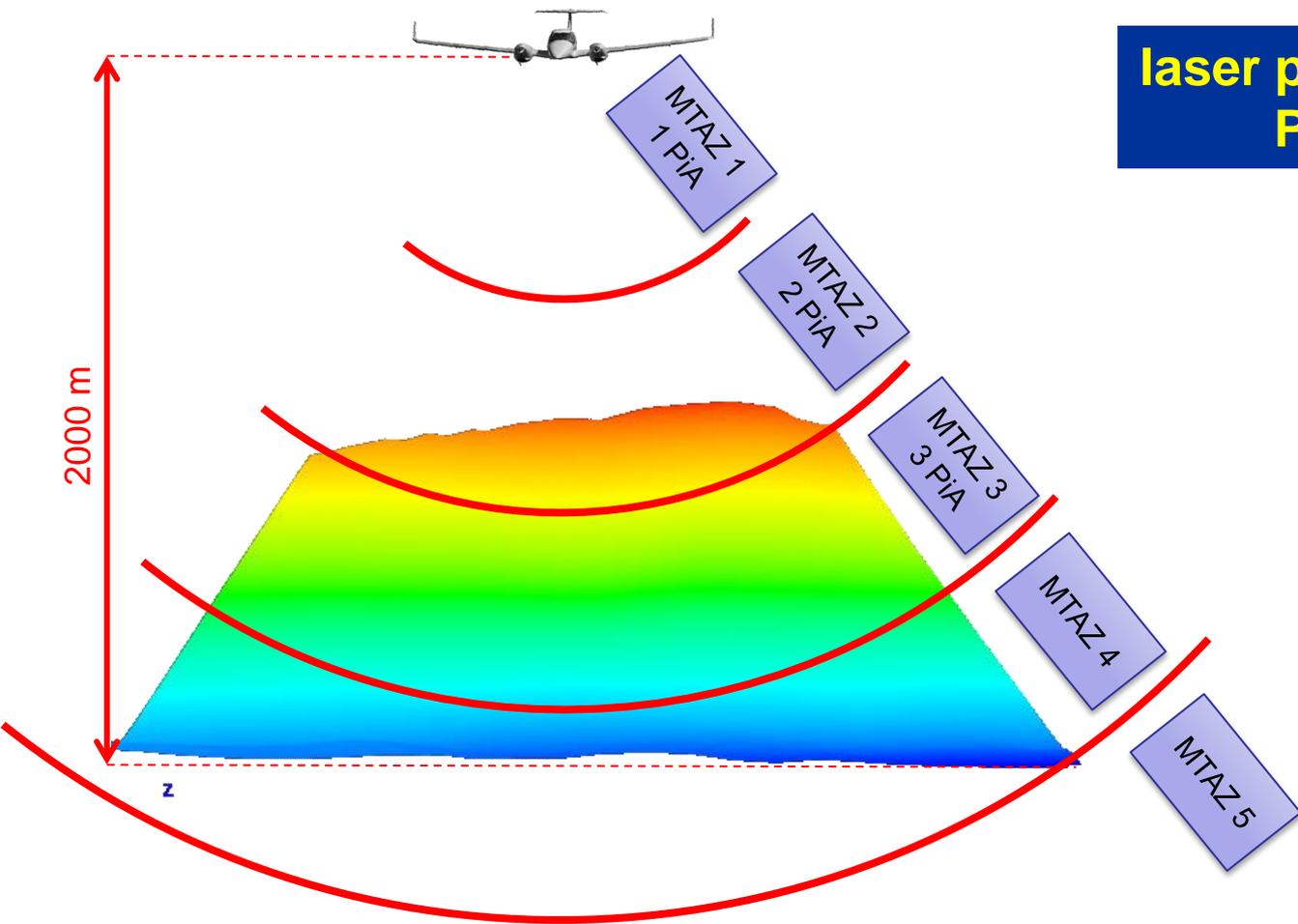


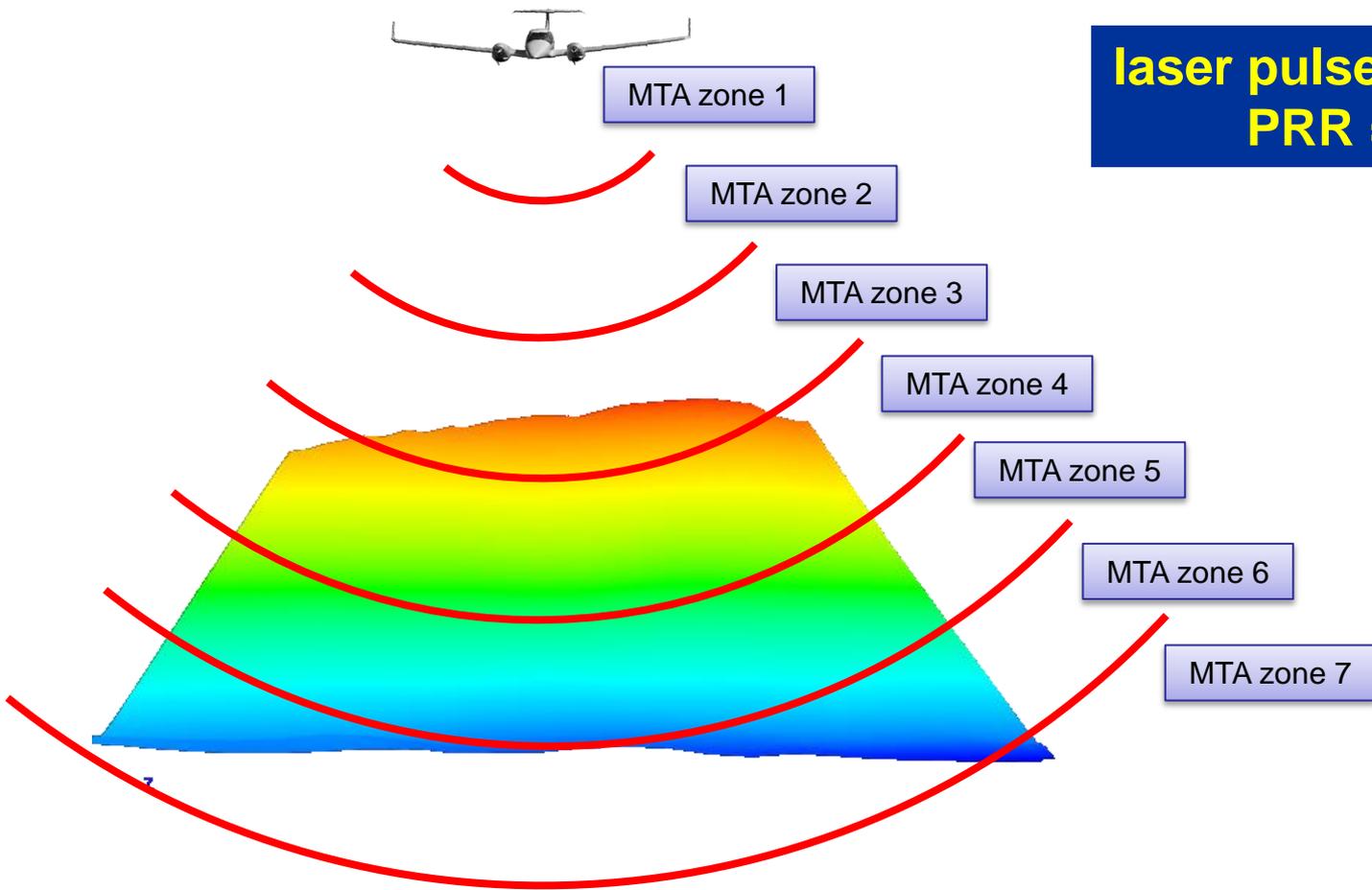
**laser pulse repetition rate  
PRR = 130 kHz**



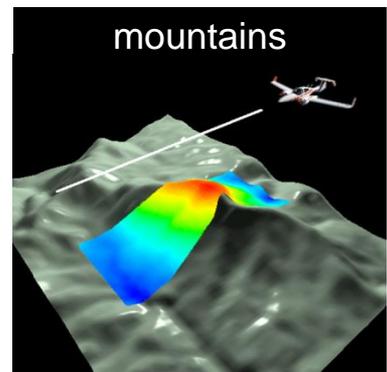


**laser pulse repetition rate  
PRR = 250 kHz**





**laser pulse repetition rate  
PRR = 400 kHz**

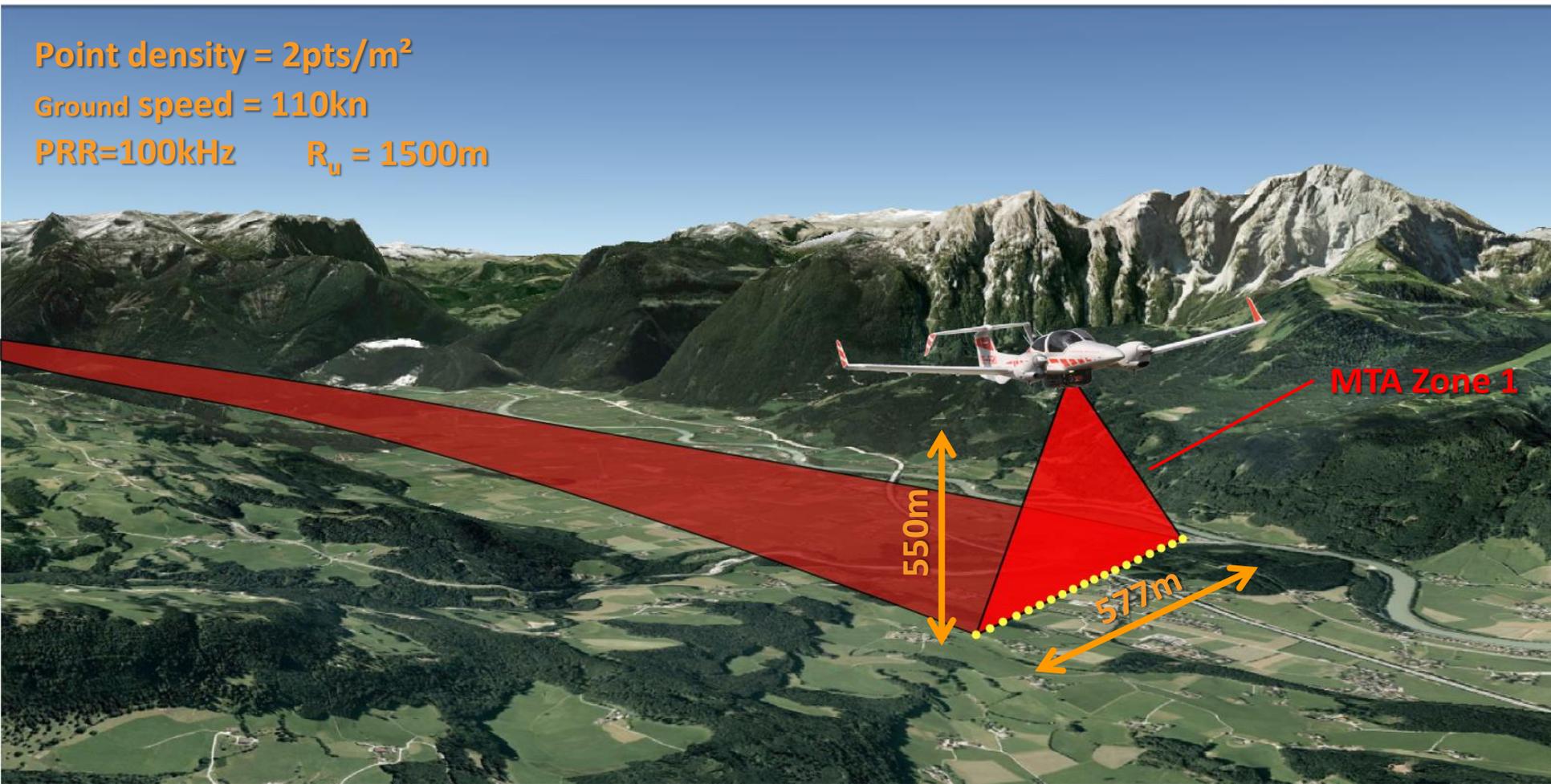




Point density = 2pts/m<sup>2</sup>

Ground speed = 110kn

PRR=100kHz     R<sub>y</sub> = 1500m



Single pulse in the air...



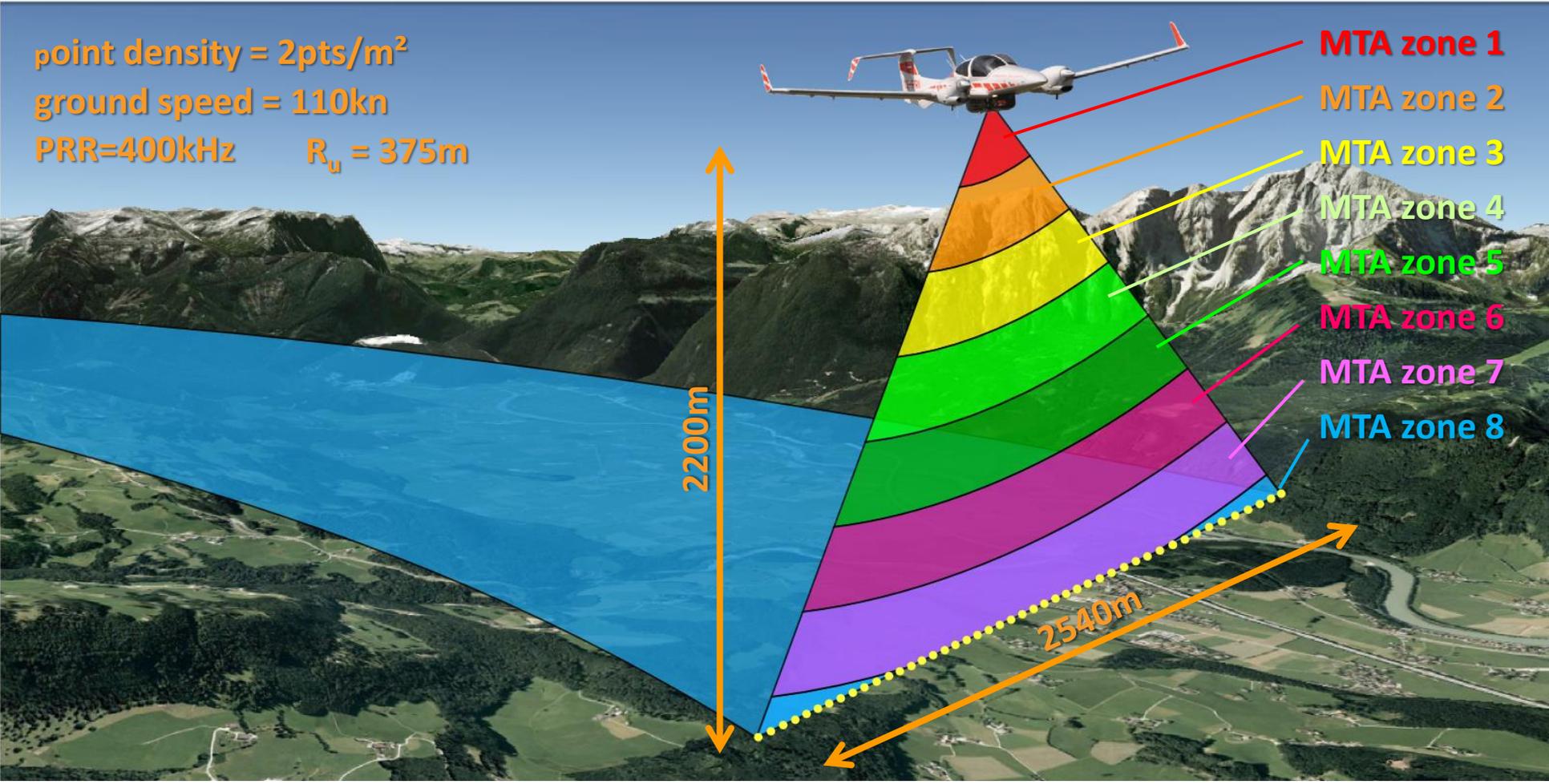
ground speed 110kn  
point density = 2 pts/m<sup>2</sup>  
PRR = 100kHz  
altitude AGL = 550m  
1 pulse in the air  
29 scan lines  
**flight time = 1 hour**

100 km<sup>2</sup>  
2 km

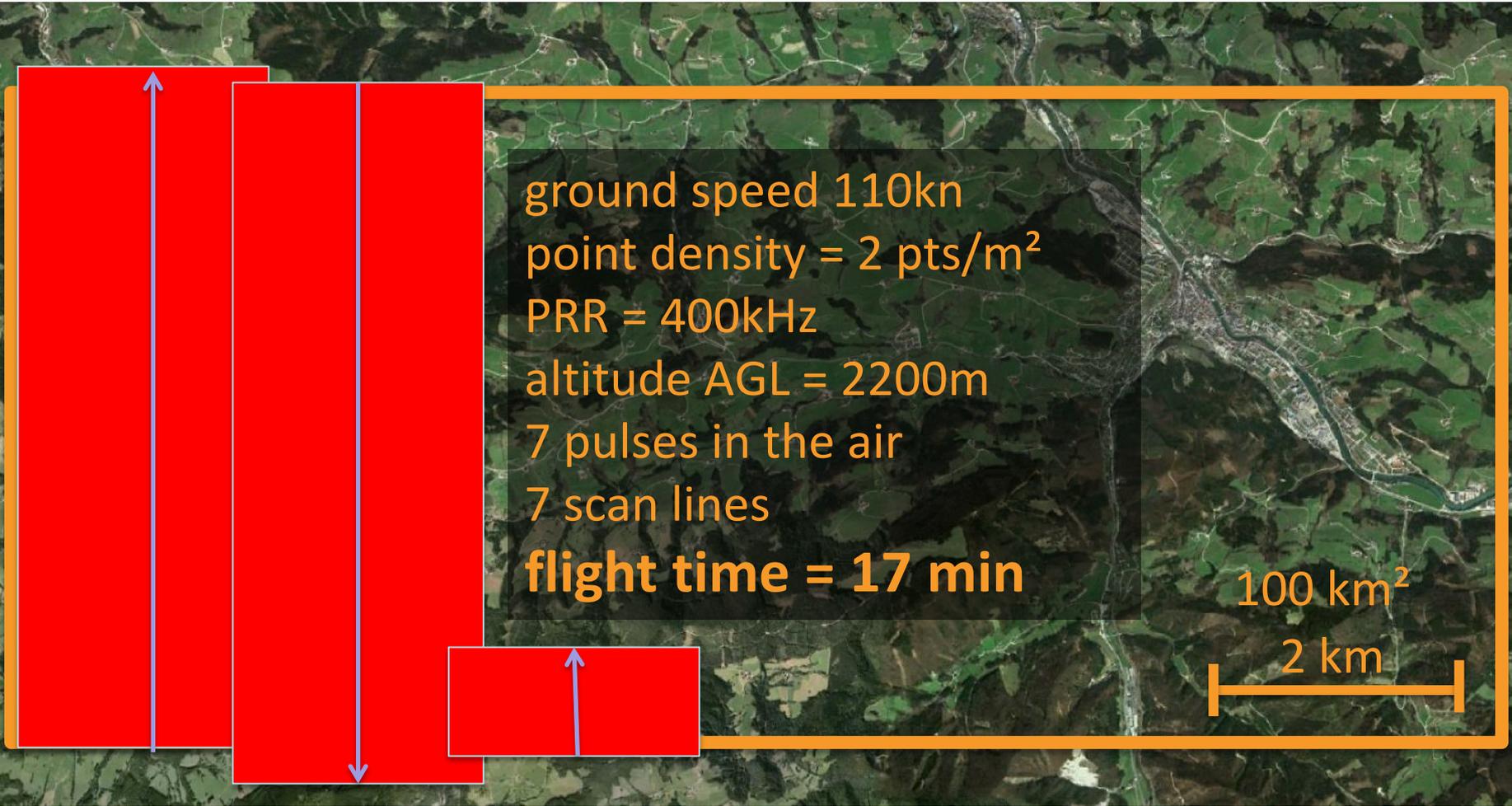




point density = 2pts/m<sup>2</sup>  
ground speed = 110kn  
PRR=400kHz     R<sub>y</sub> = 375m



Multiple pulses in the air...



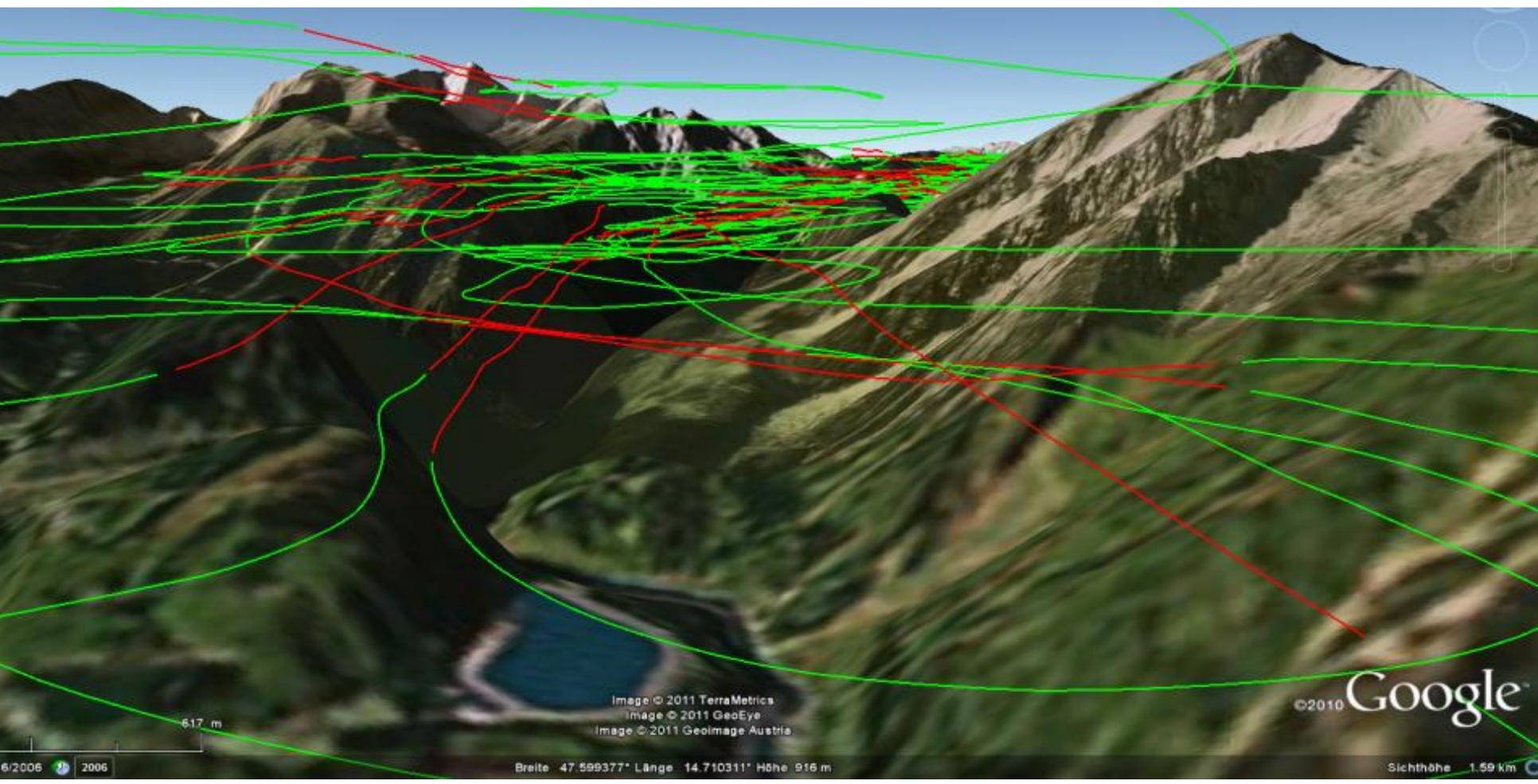


PRR = 100kHz

$R_v = \text{max. range} = 1500\text{m}$



Single pulse in the air...

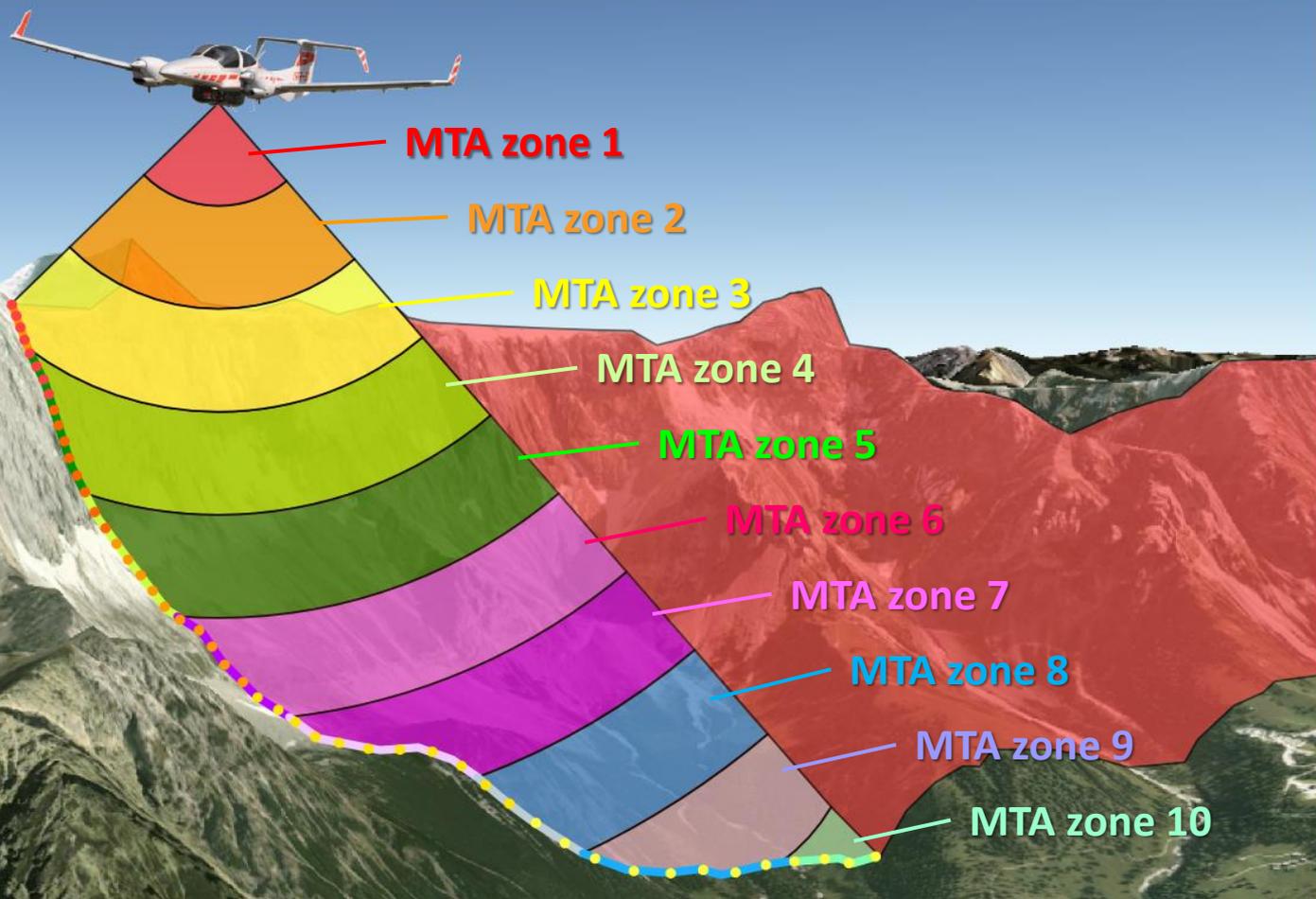


...difficult flights

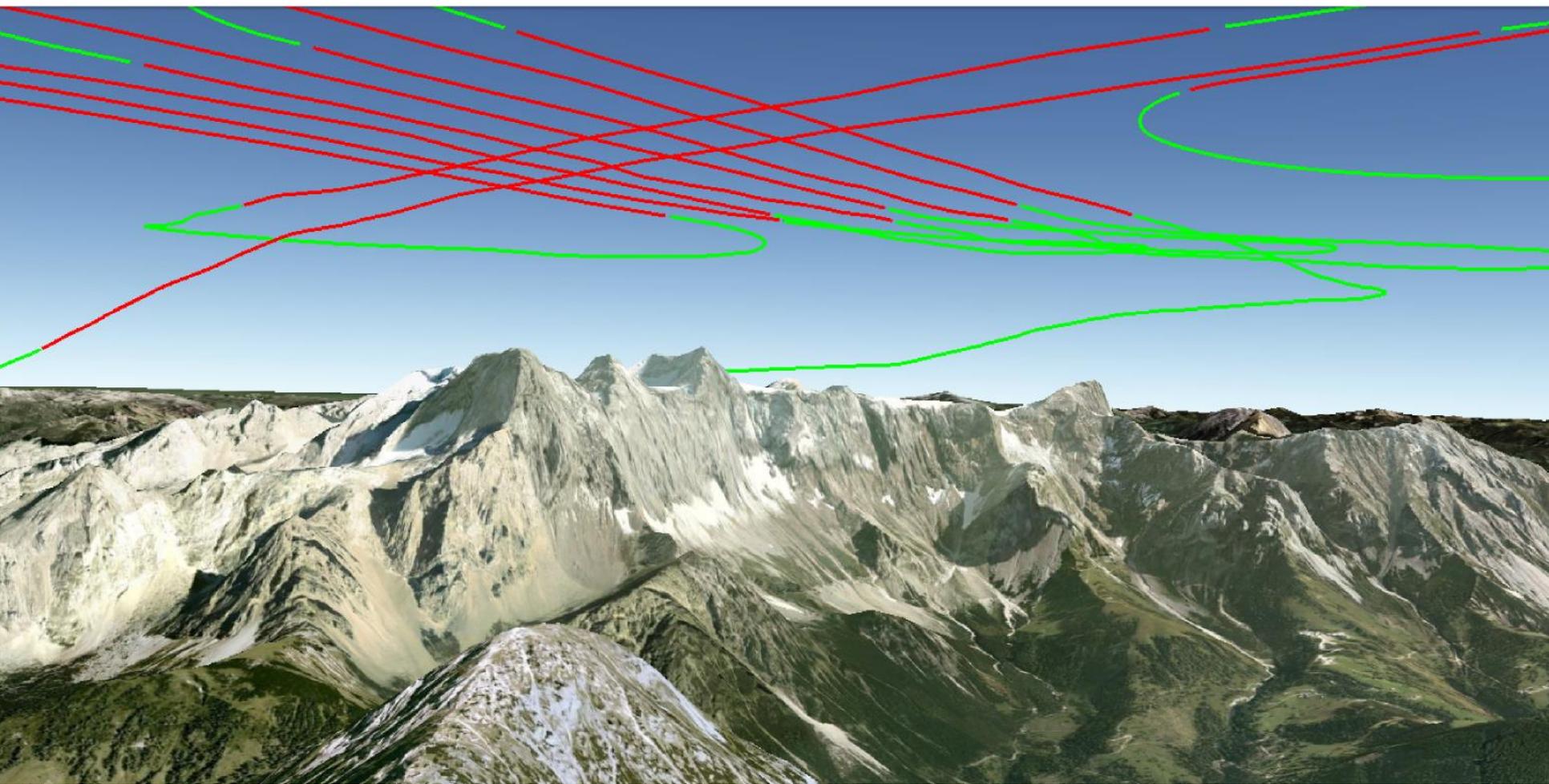


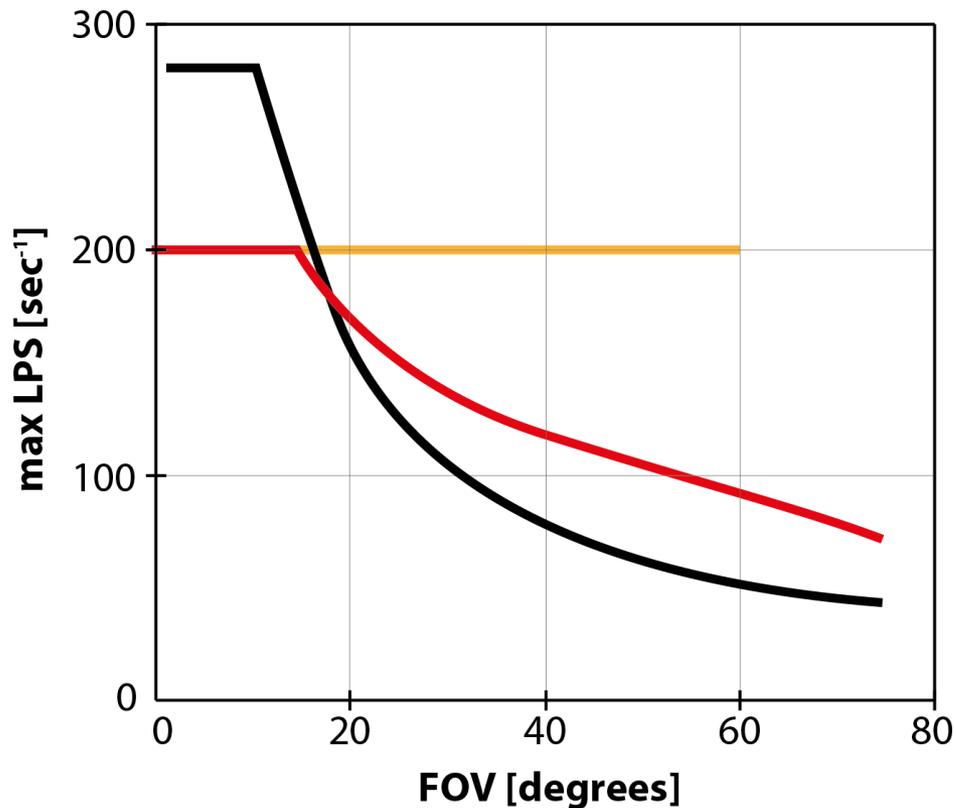
PRR = 400kHz

$R_v = 375m$



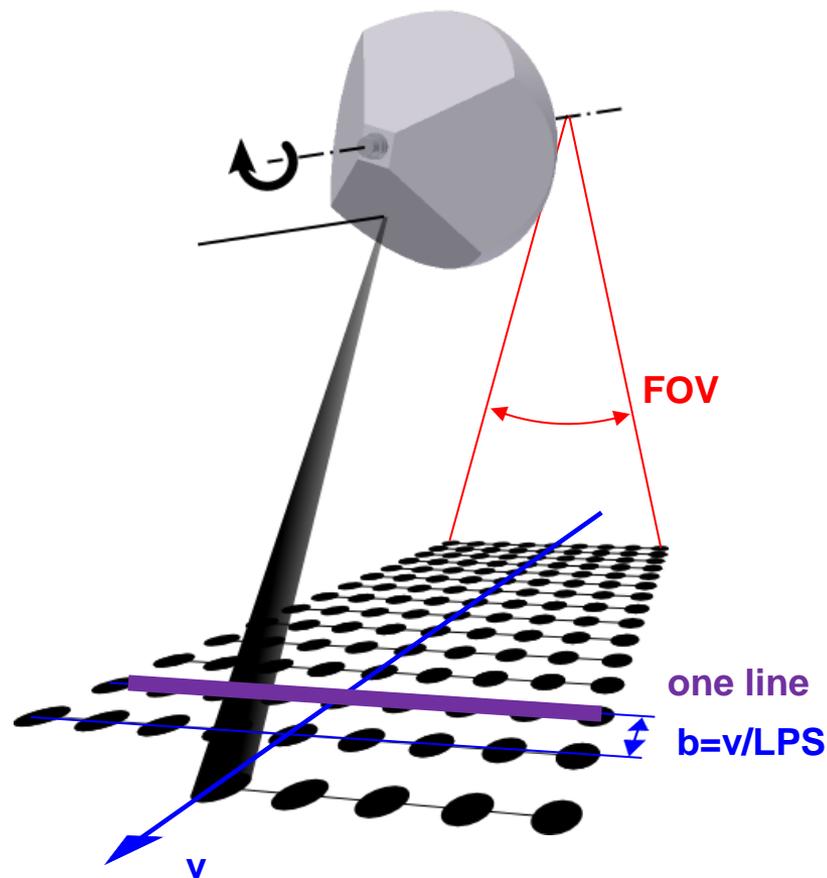
multiple pulses in the air

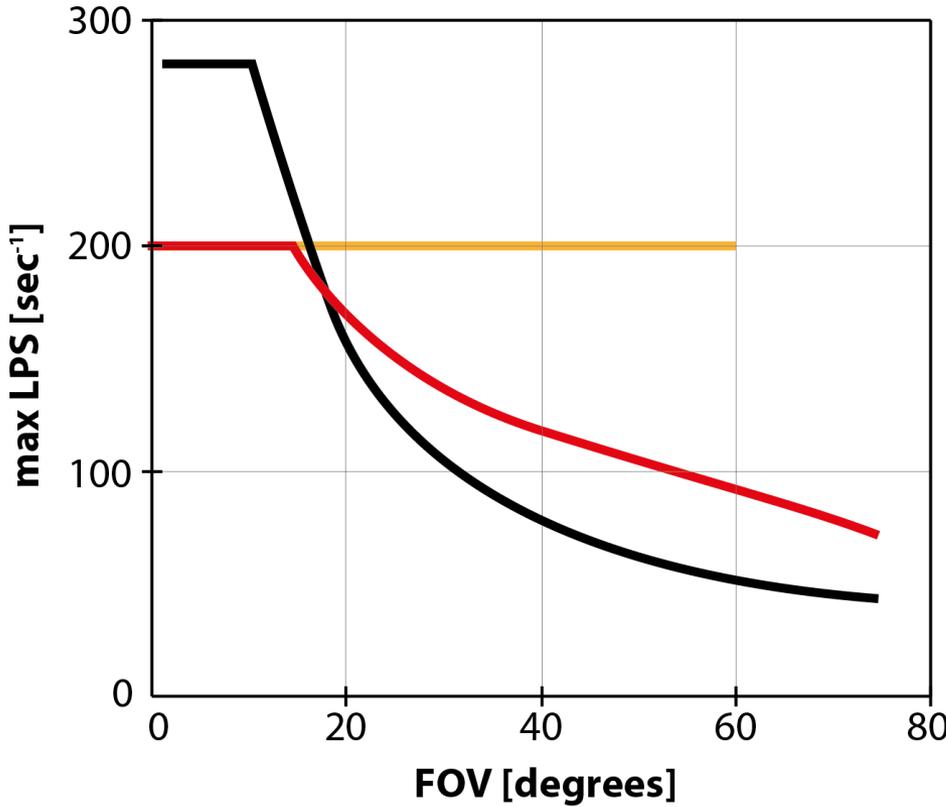




- instrument A, *RIEGL LMS-Q780*
- instrument B (single channel)
- instrument C (single channel)

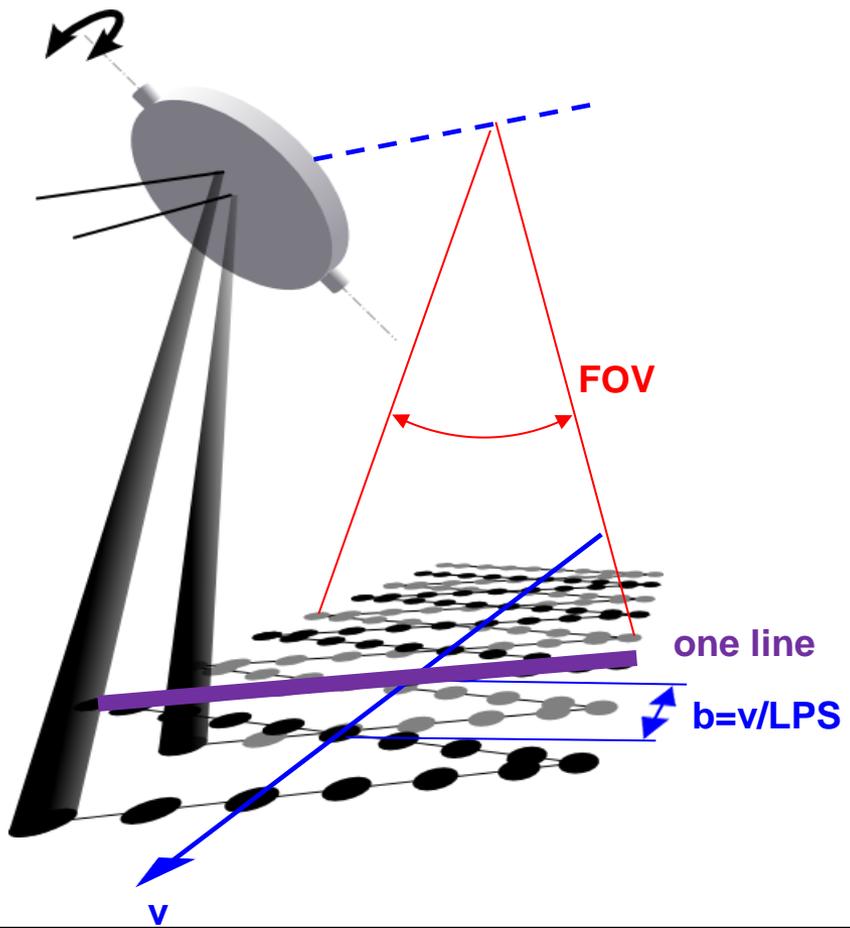
FOV .. field of view, LPS... lines per second, v .. speed over ground, b .. line spacing

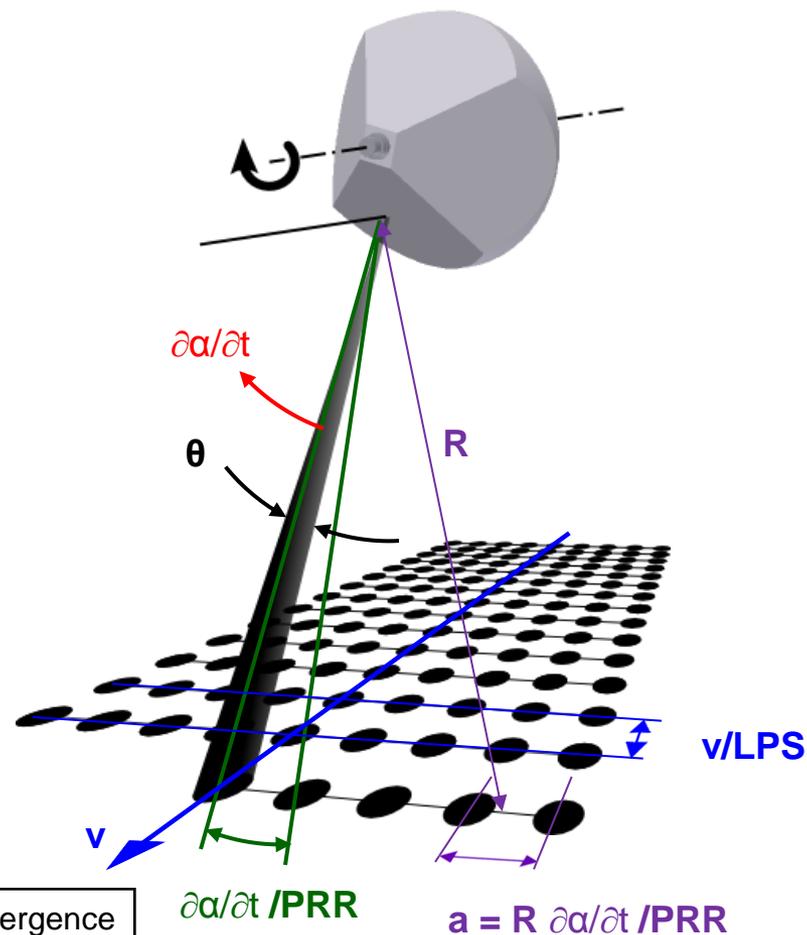
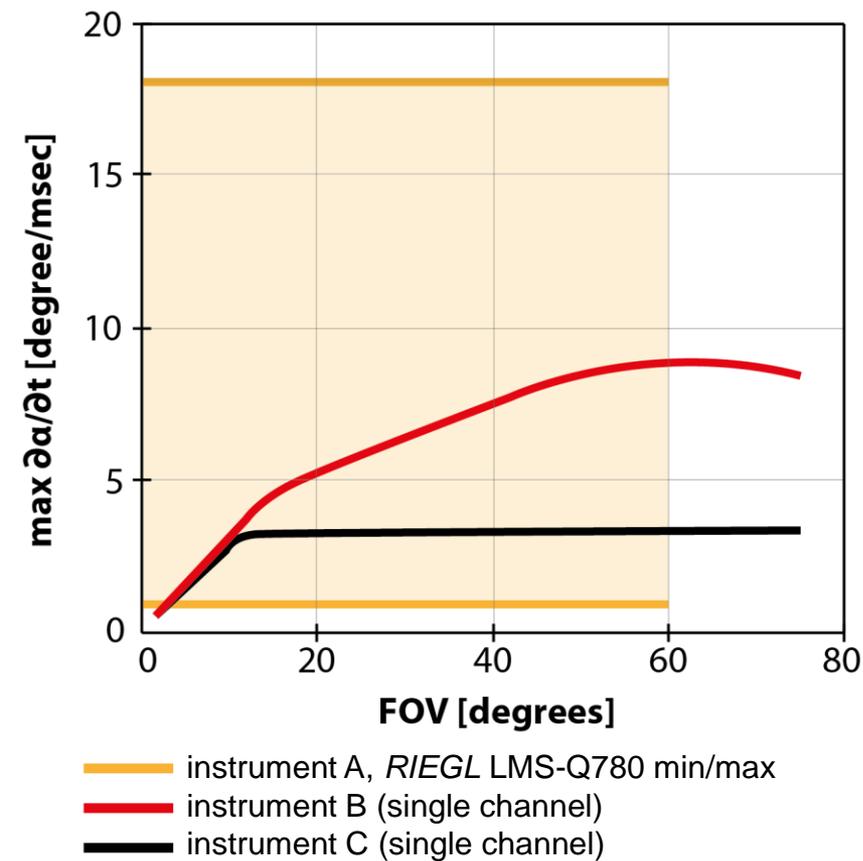




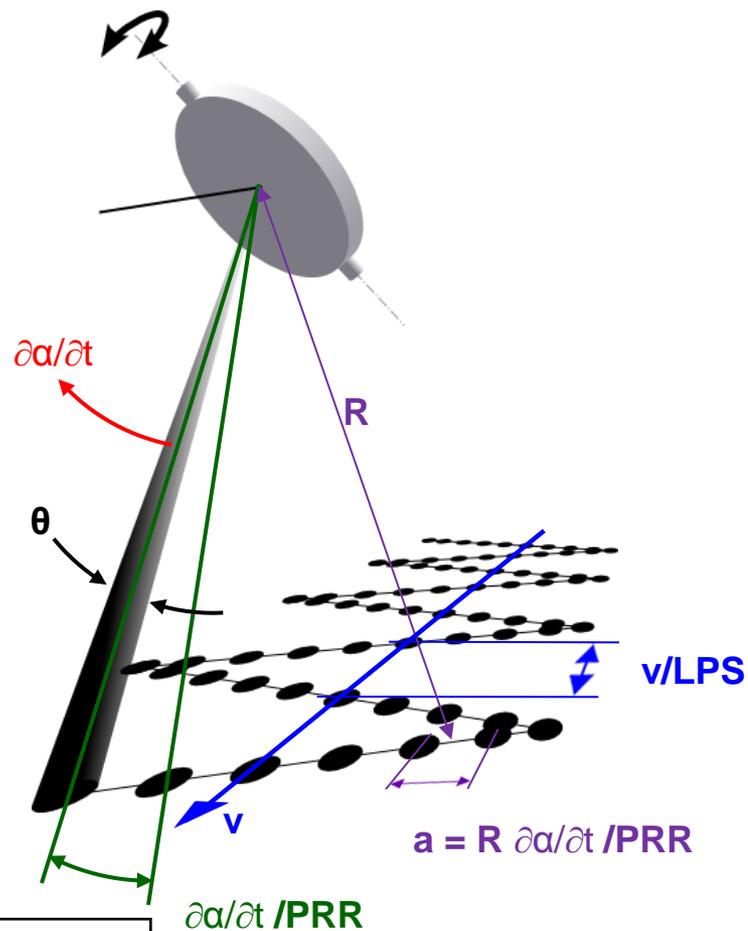
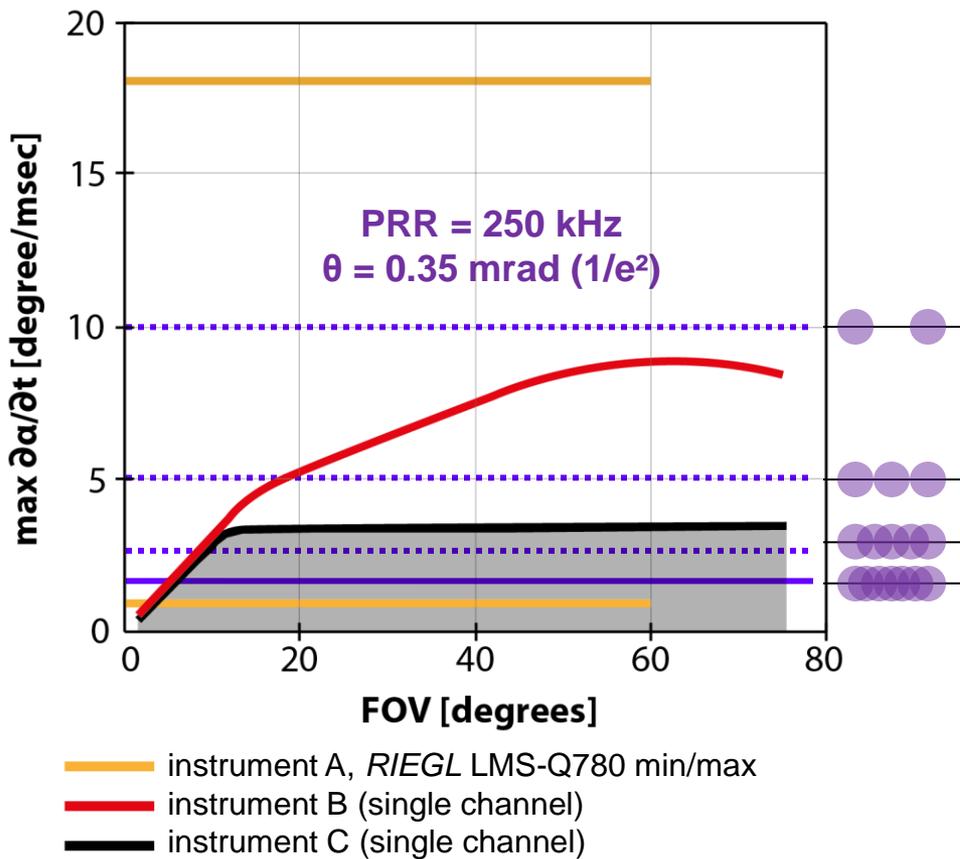
- instrument A, *RIEGL LMS-Q780*
- instrument B (single channel)
- instrument C (single channel)

FOV .. field of view, LPS... lines per second, v .. speed over ground, b .. line spacing

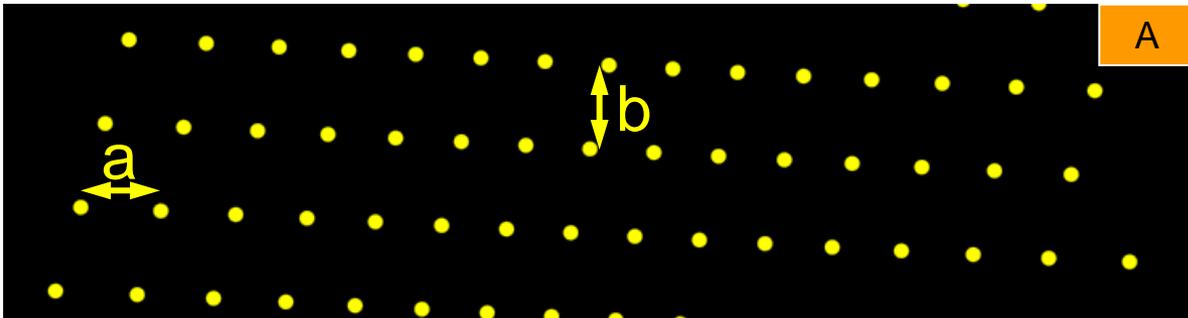




$\partial\alpha/\partial t$ ... angular speed, PRR... laser pulse repetition rate,  $\theta$  .. beam divergence

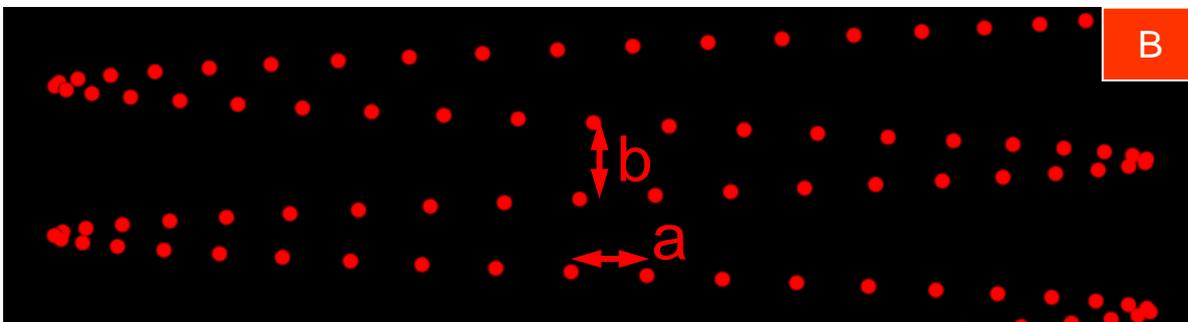


$\partial\alpha/\partial t$ ... angular speed, PRR... laser pulse repetition rate,  $\theta$  .. beam divergence

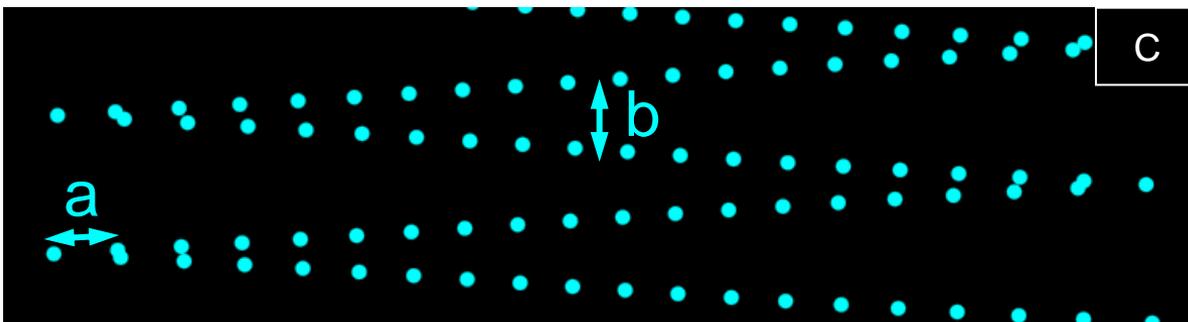


$$a = b \Rightarrow$$

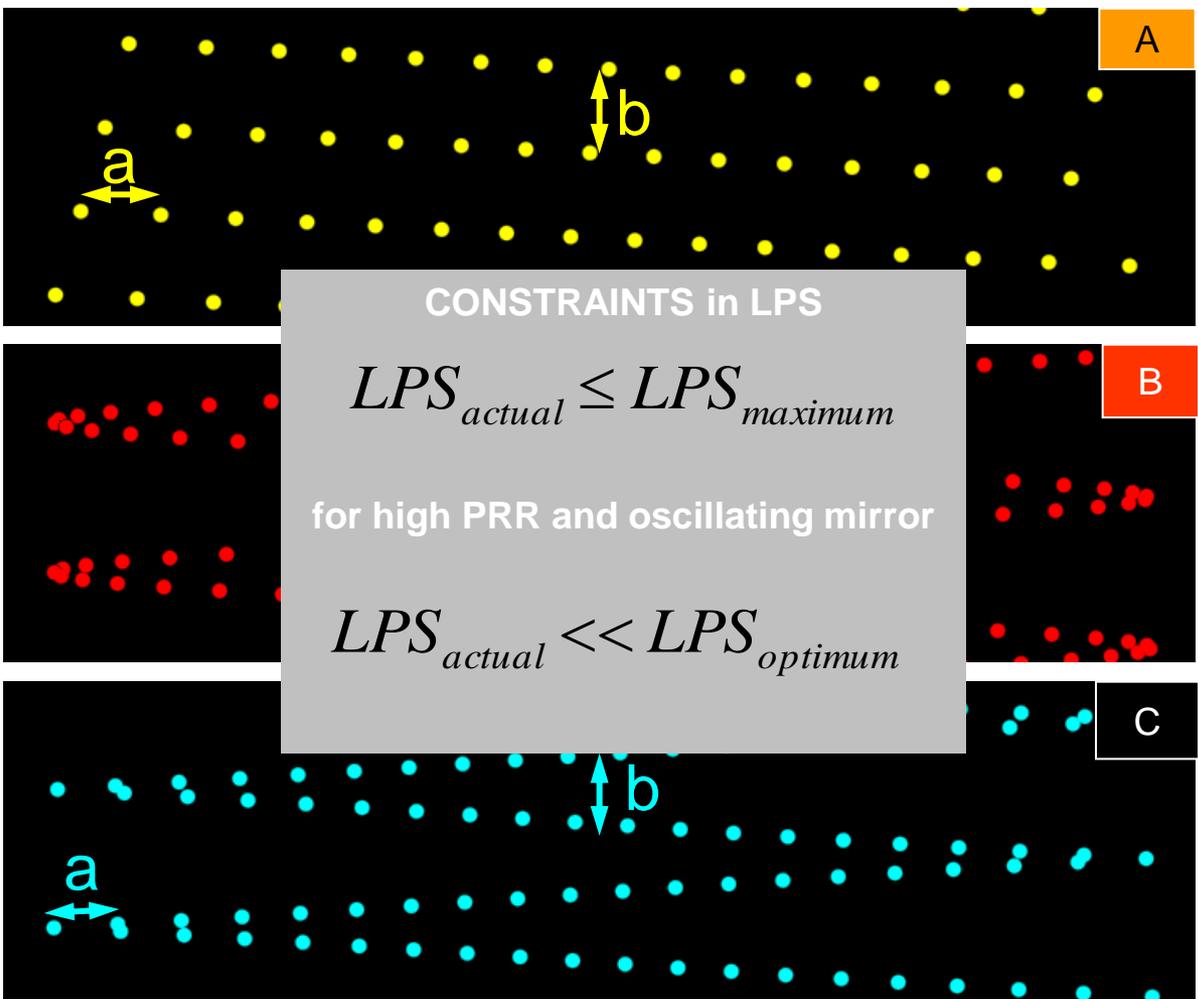
$$LPS_{optimum} = \cos\left(\frac{FOV}{2}\right) \sqrt{\frac{2}{\pi}} \sqrt{\frac{v.PRR}{AGL}}$$



$$LPS_{optimum} = \sqrt{\frac{2}{\pi.FOV}} \sqrt{\frac{v.PRR}{AGL}}$$



$$LPS_{optimum} = \cos\left(\frac{FOV}{2}\right) \sqrt{\frac{1}{FOV}} \sqrt{\frac{v.PRR}{AGL}}$$



**CONSTRAINTS in LPS**

$$LPS_{actual} \leq LPS_{maximum}$$

for high PRR and oscillating mirror

$$LPS_{actual} \ll LPS_{optimum}$$

$$a = b \Rightarrow$$

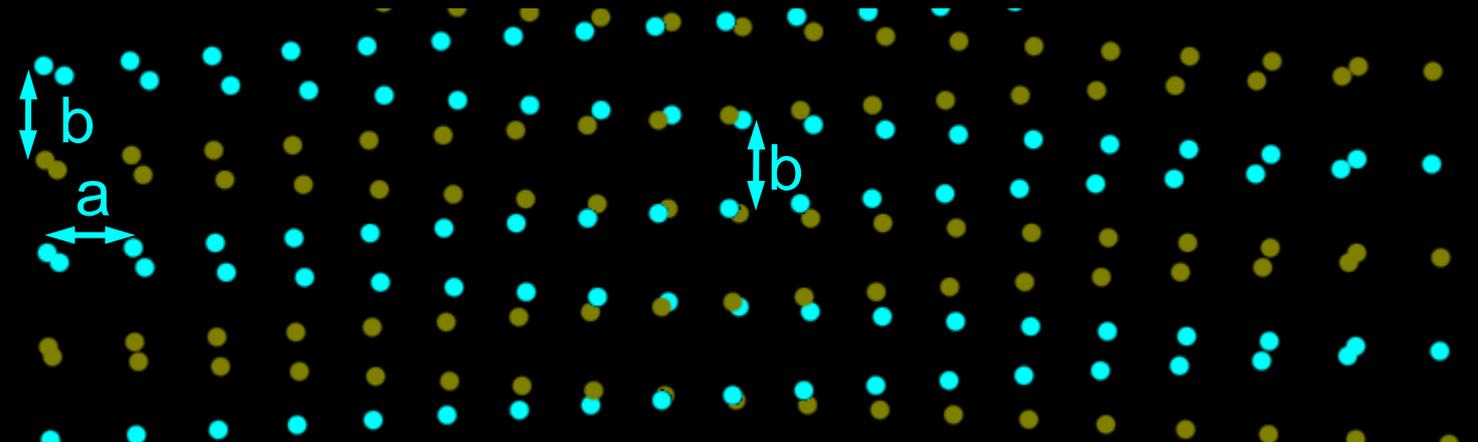
$$LPS_{optimum} = \cos\left(\frac{FOV}{2}\right) \sqrt{\frac{2}{\pi}} \sqrt{\frac{v.PRR}{AGL}}$$

$$LPS_{optimum} = \sqrt{\frac{2}{\pi.FOV}} \sqrt{\frac{v.PRR}{AGL}}$$

$$LPS_{optimum} = \cos\left(\frac{FOV}{2}\right) \sqrt{\frac{1}{FOV}} \sqrt{\frac{v.PRR}{AGL}}$$

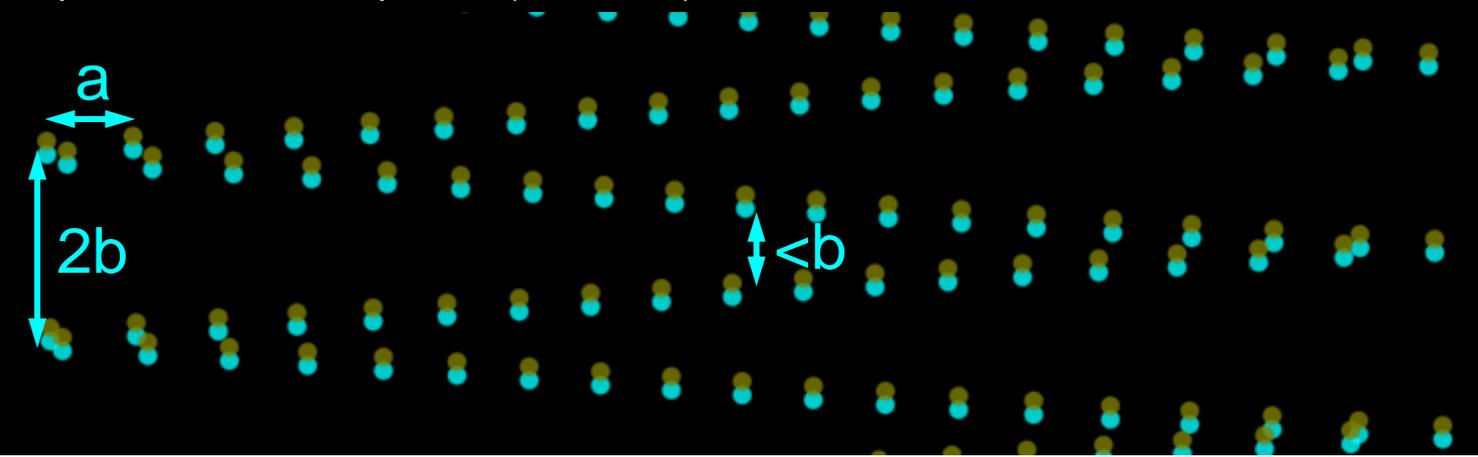


out-of-phase interference pattern (desired)



- phase depends on
- speed
  - AGL
  - LPS

in-phase interference pattern (undesired)

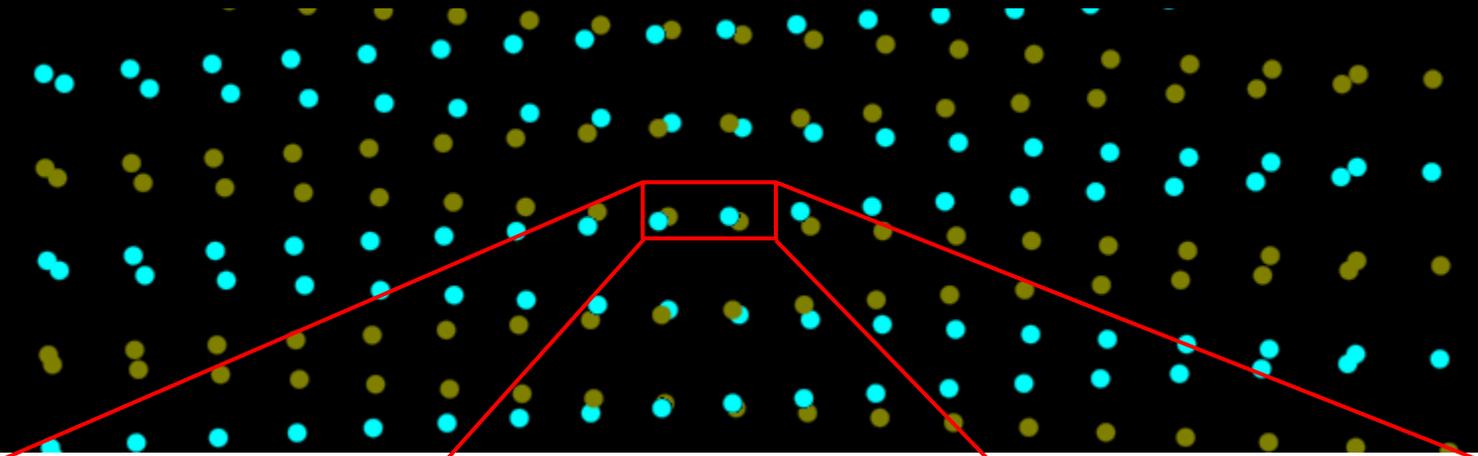


in any case:  
2x “point density”

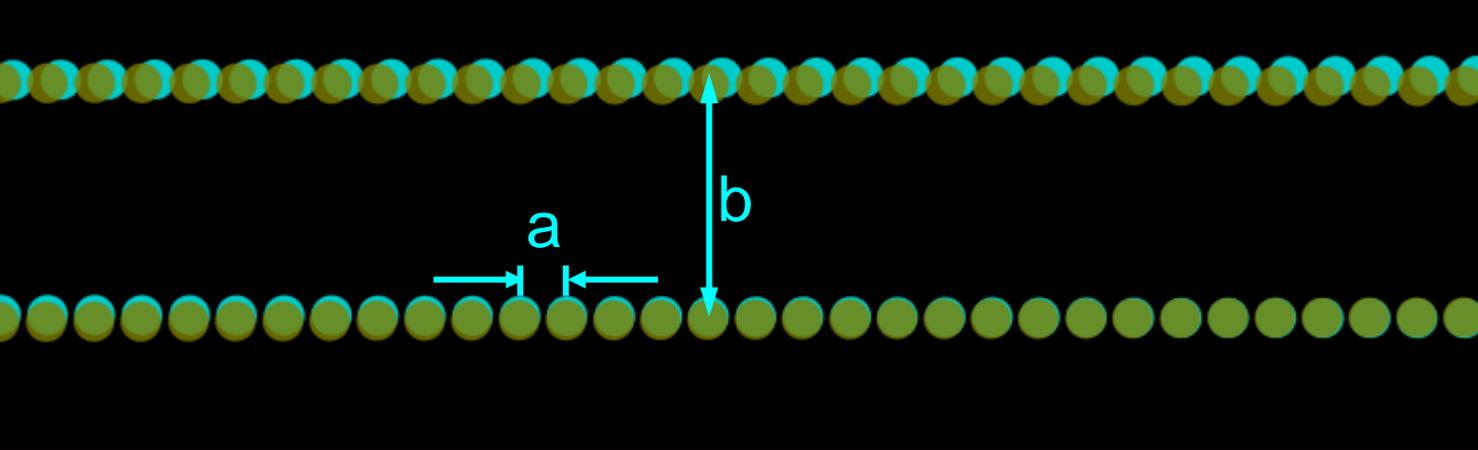
but:  
“point spacing” ?



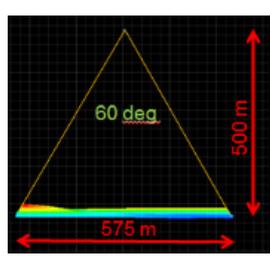
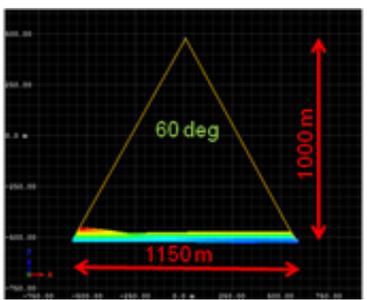
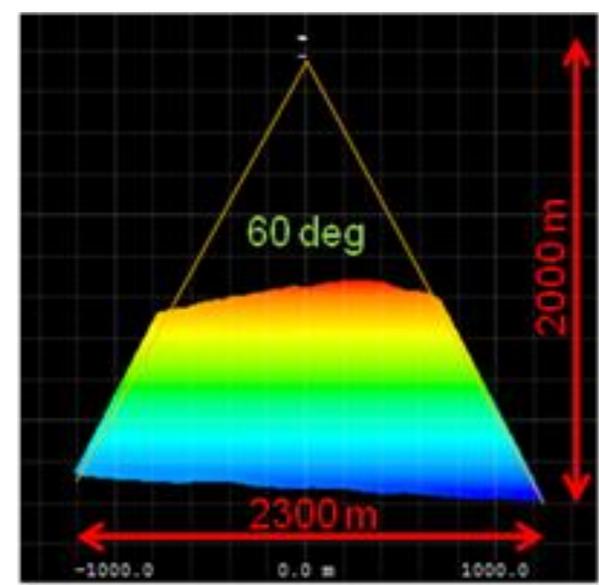
1 LPS, 60 deg FOV, PRR 20 Hz ... just a sketch

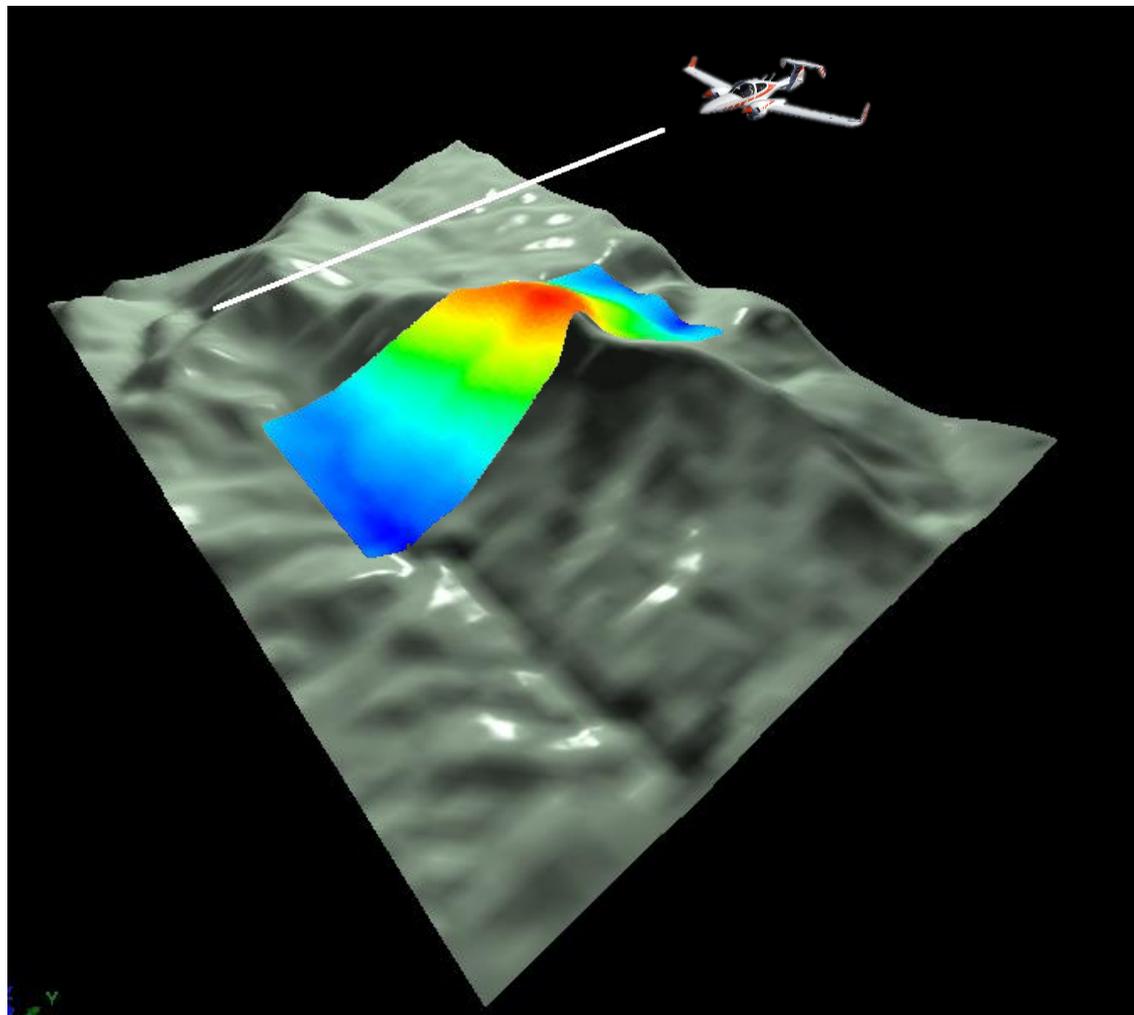


27 LPS, 60 deg FOV, PRR 50 kHz





	scenario 1	scenario 2	scenario 3
<b>application</b>	corridor mapping	high density survey	wide area mapping
<b>terrain</b>	flat	flat	mountainous
<b>AGL</b>	500 m	1000 m	2000 m – 1000 m
<b>speed</b>	60 kn	120 kn	140 kn
<b>FOV</b>	60 deg	60 deg	60 deg
			



mountainous terrain

- variation in AMSL 1000 m
- scenario 3



defining test area (scenarios 1 – 3)

choosing optimum flight parameters

performance envelope  $\rightarrow$   $PRR_{max}$

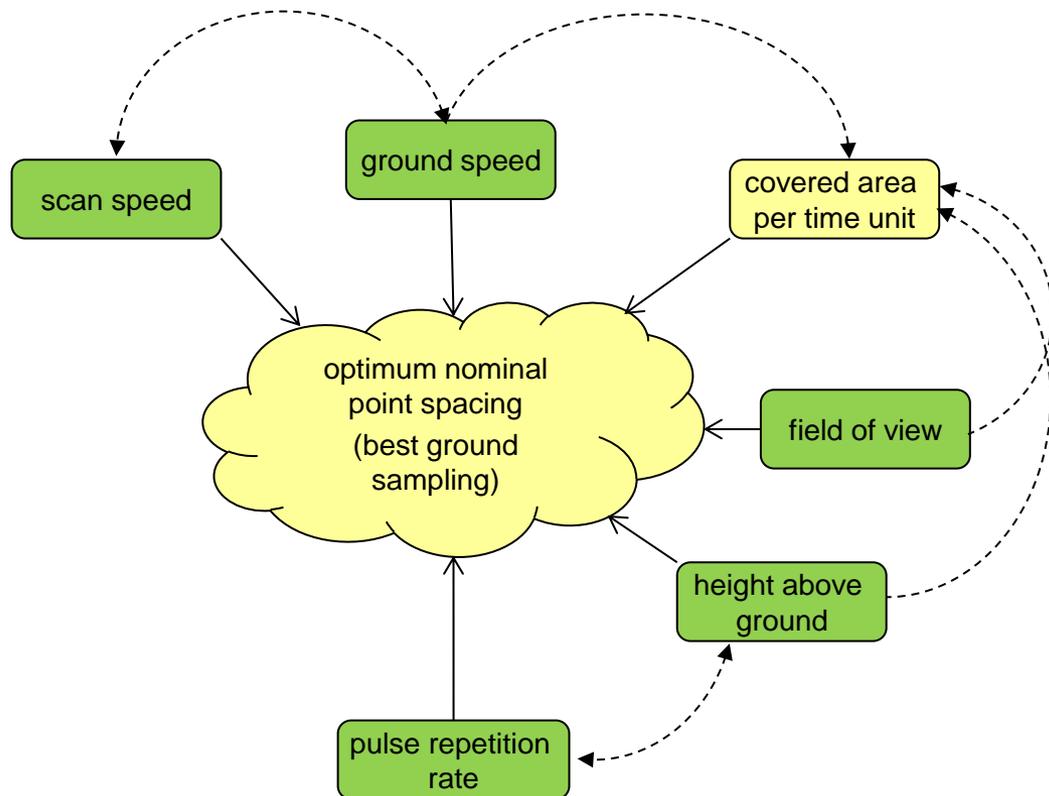
calculating  $LPS_{optimum} \rightarrow LPS_{actual}$

generating trajectory

“mounting” LIDAR &  
generating “pulses”

intersecting beams with terrain

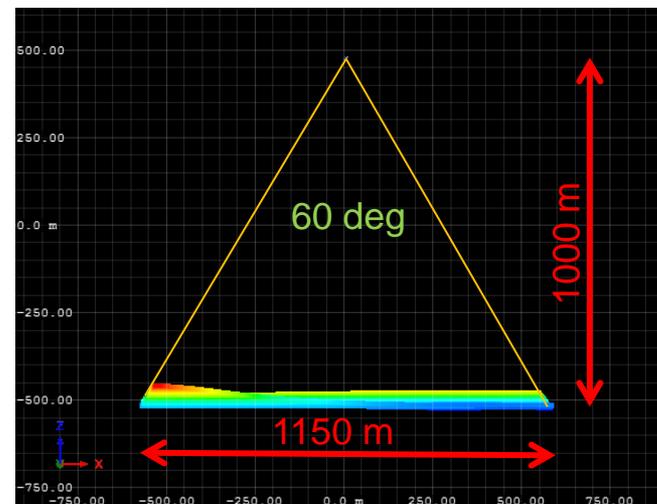
analyzing / visualizing point clouds



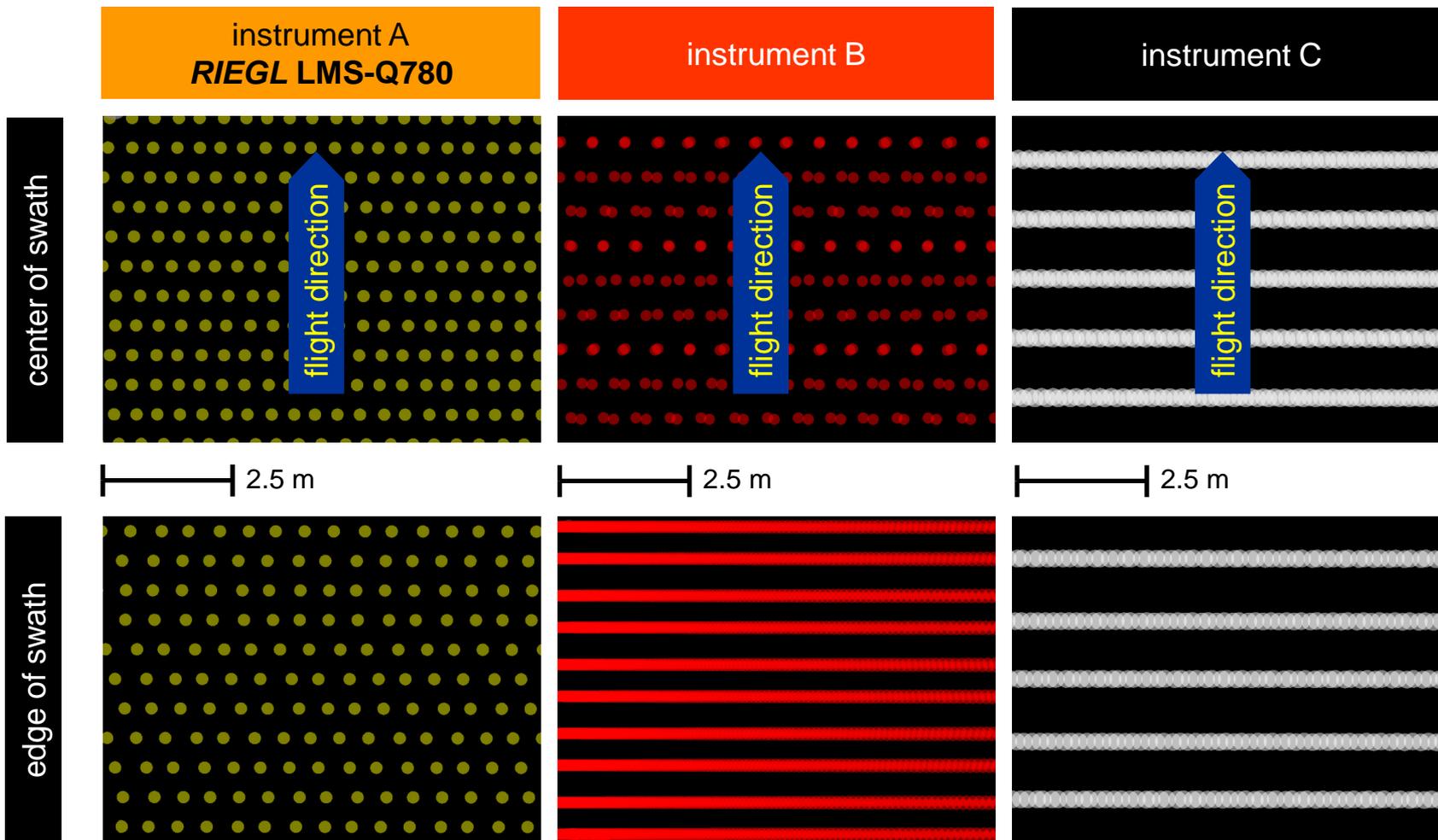


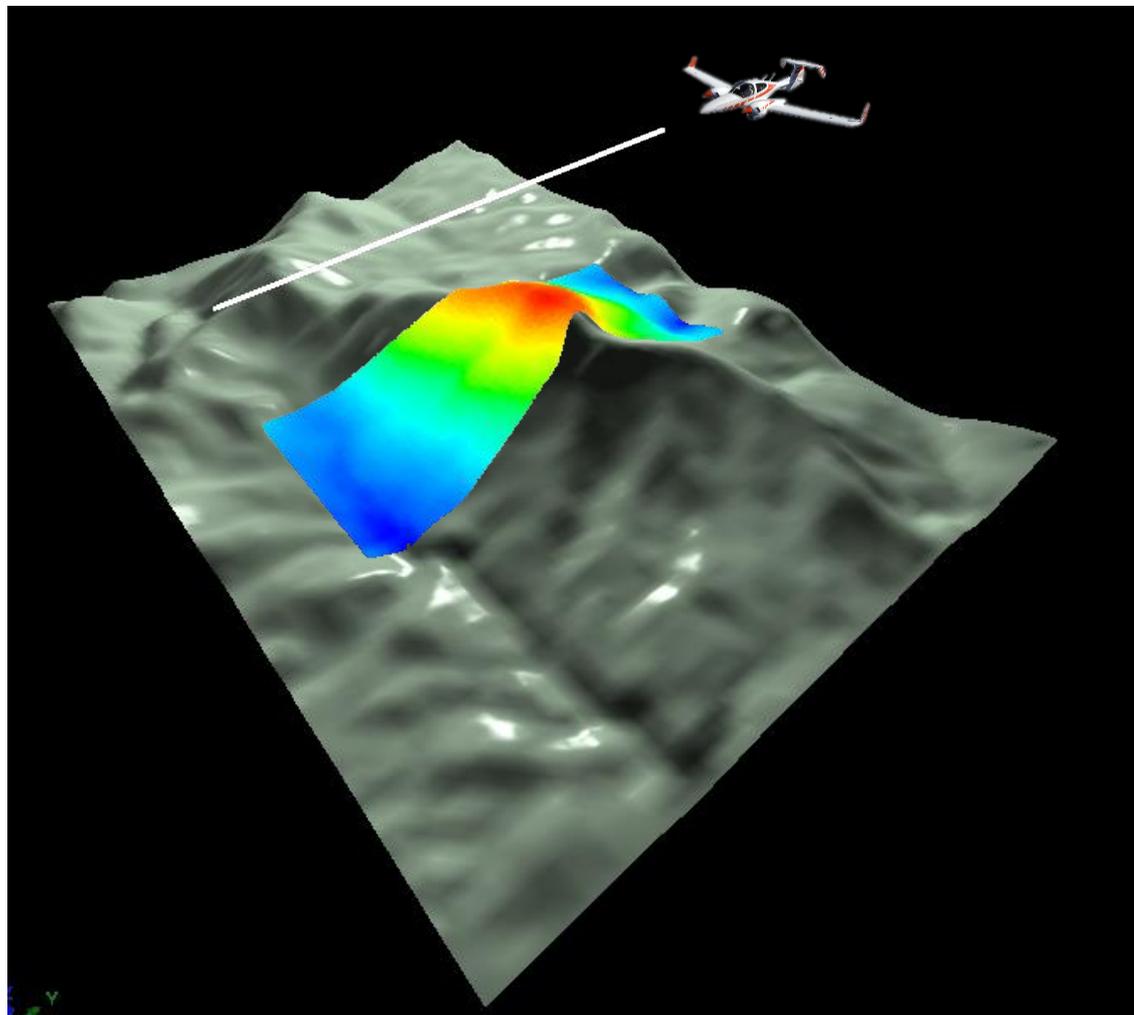
## Performance on flat terrain

- AGL at 1000 m
- speed over ground 120 kn
- FOV of 60 degrees
- optimum operating parameters for all instruments



	AGL	FOV	MR	LPS	across spacing	along spacing	point density
<b>instrument A</b>	1000 m	60 deg	1x 266 kHz	1x 108 LPS	0.57 m	0.57 m	4.1 p/m <sup>2</sup>
<b>instrument B</b>	1000 m	60 deg	2x 250 kHz	2x 93 LPS	0.61 m	0.66 m	7.7 p/m <sup>2</sup>
<b>instrument C</b>	1000 m	60 deg	2x 250 kHz	2x <b>53 LPS</b>	0.30 m	<b>1.16 m</b>	7.7 p/m <sup>2</sup>





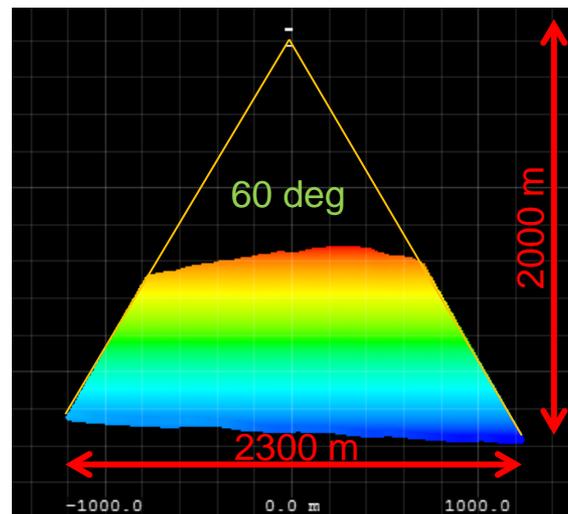
mountainous terrain

- variation in AMSL 1000 m
- scenario 3

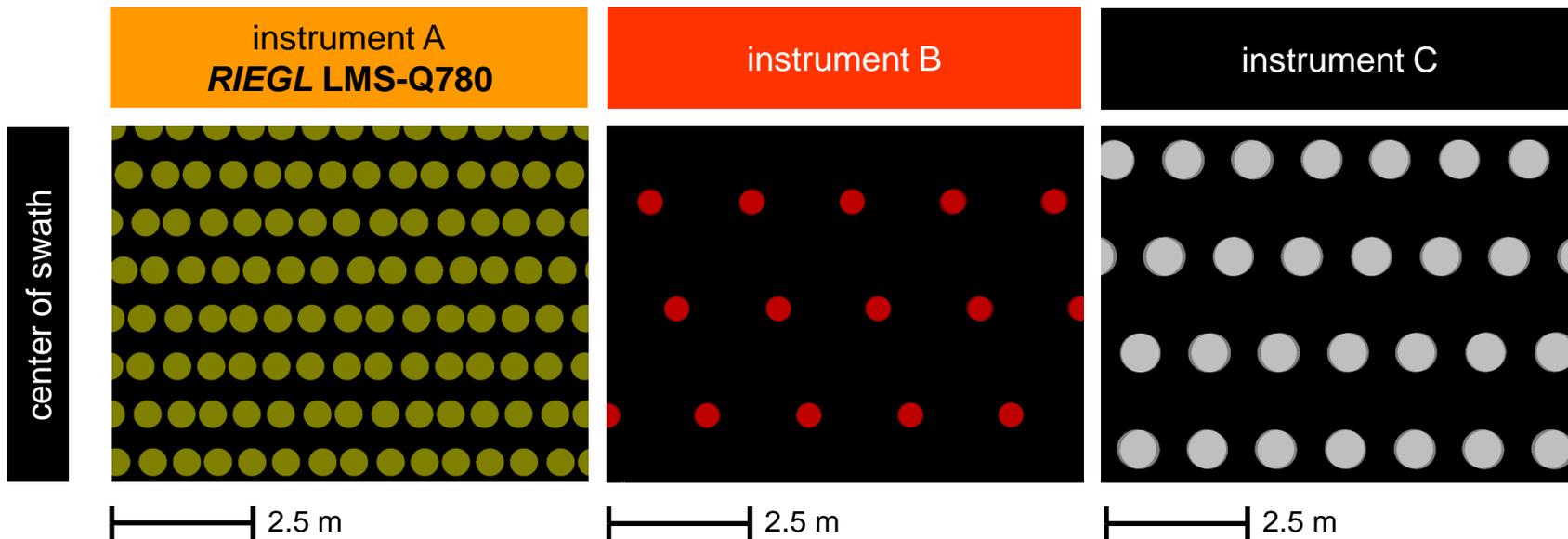


## Performance on mountainous terrain

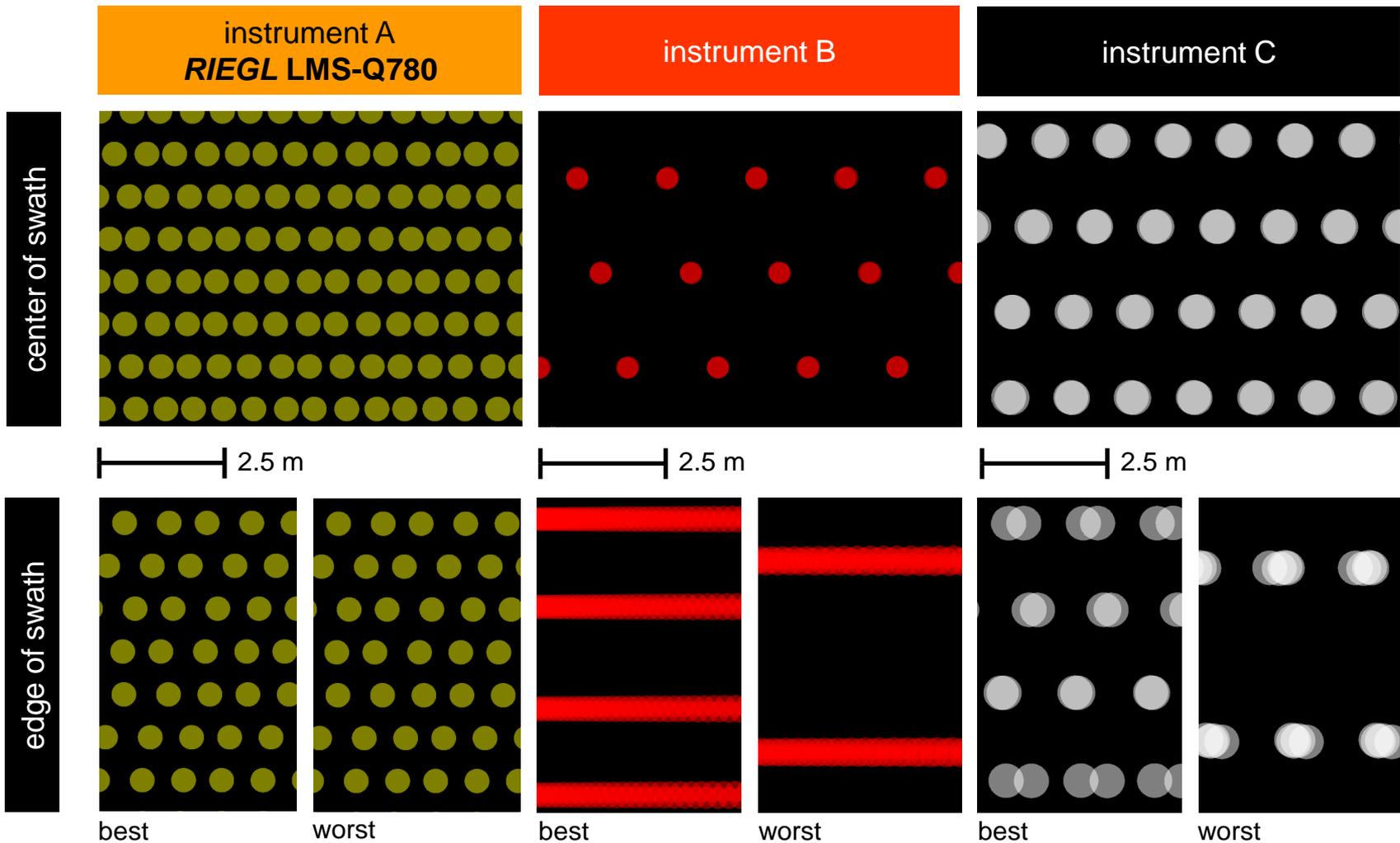
- AGL from 1000 m to 2000 m
- speed over ground 140 kn
- FOV of 60 degrees
- optimum operating parameters for all instruments

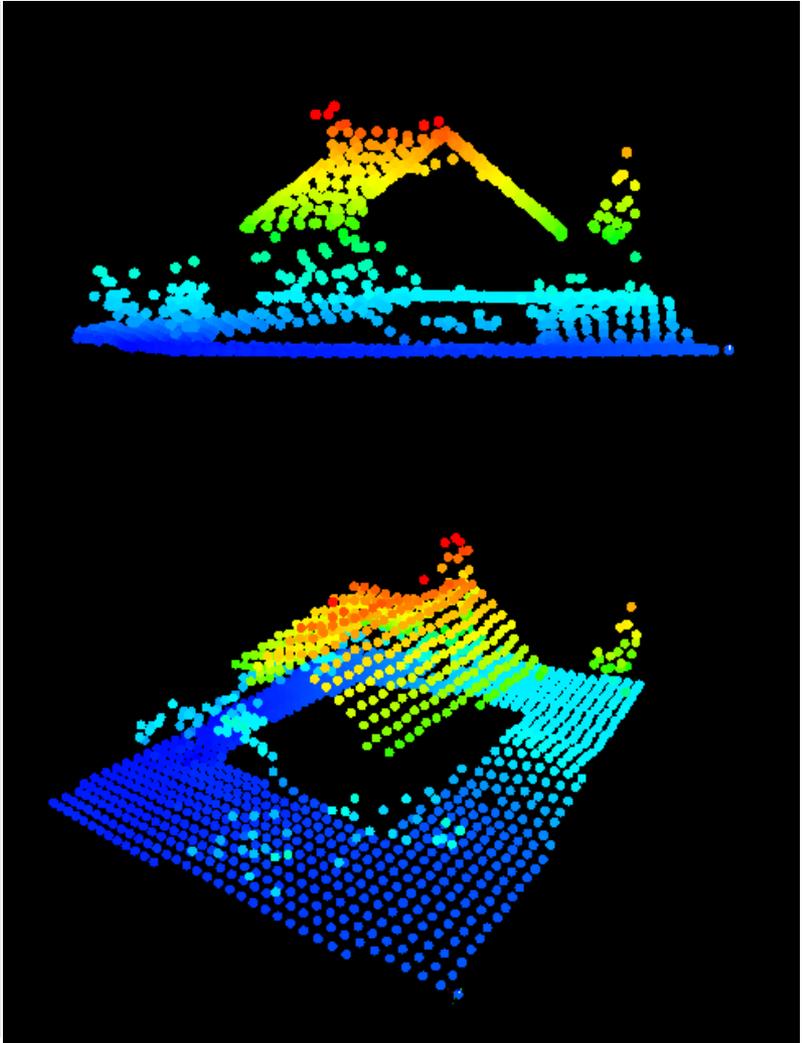
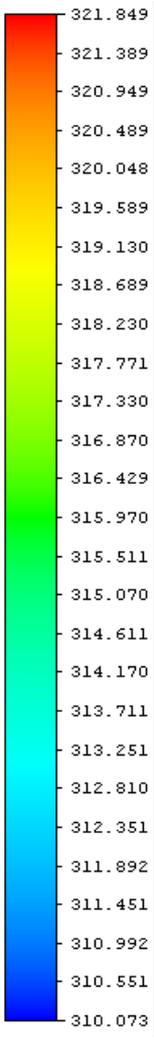
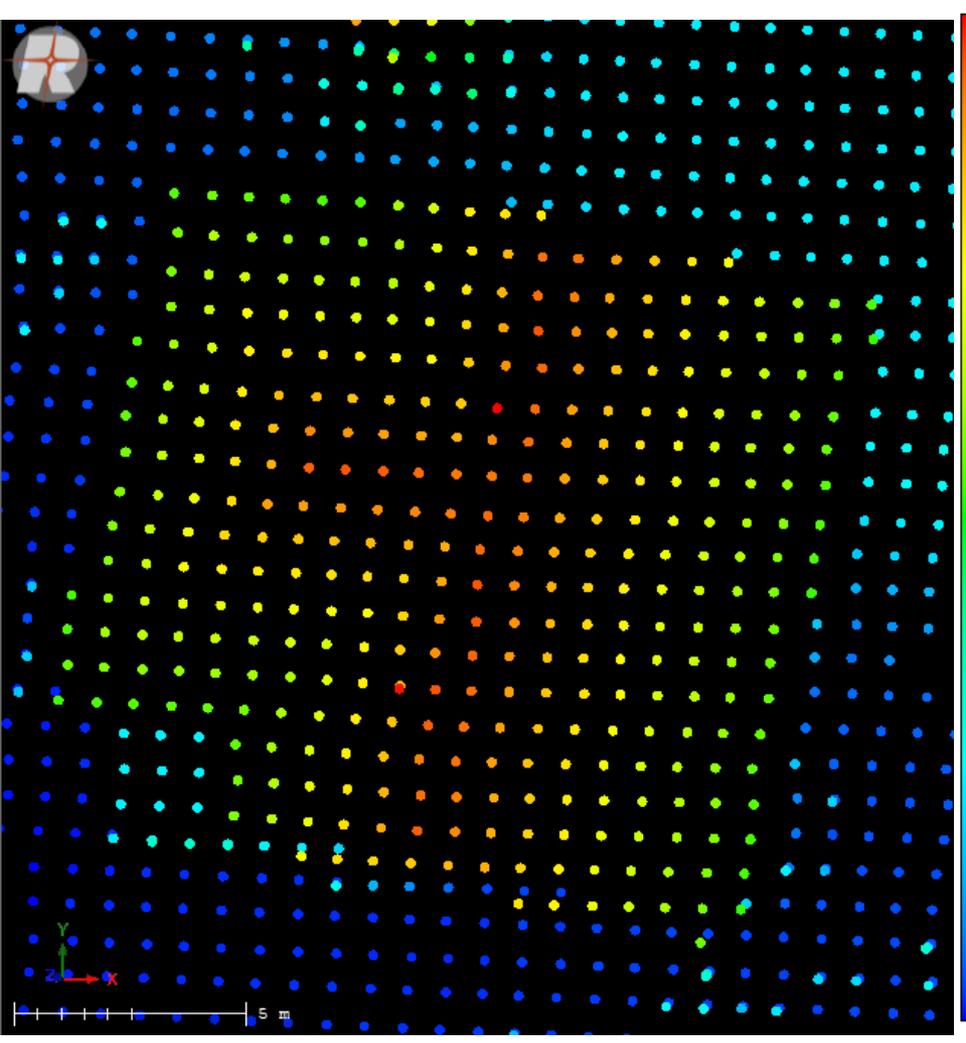


	maximum AGL	FOV	meas. rate	LPS	across spacing	along spacing	avg. point density
<b>instrument A</b>	2000 m	60 deg	1x 266 kHz	1x 83 LPS	0.87 m	0.87 m	1.3 - 3.5 p/m <sup>2</sup>
<b>instrument B</b>	2000 m	60 deg	2x 63 kHz	2x 37 LPS	1.94 m	4.32 m	0.53 - 1.9 p/m <sup>2</sup>
<b>instrument C</b>	2000 m	60 deg	2x 66 kHz	2x 41 LPS	1.74 m	3.50 m	0.9 - 2.6 p/m <sup>2</sup>



- variation in terrain height permits only acquisition in MTA zone 1 (1 pulse in the air)
- dead time between zones reduces measurement rate even further



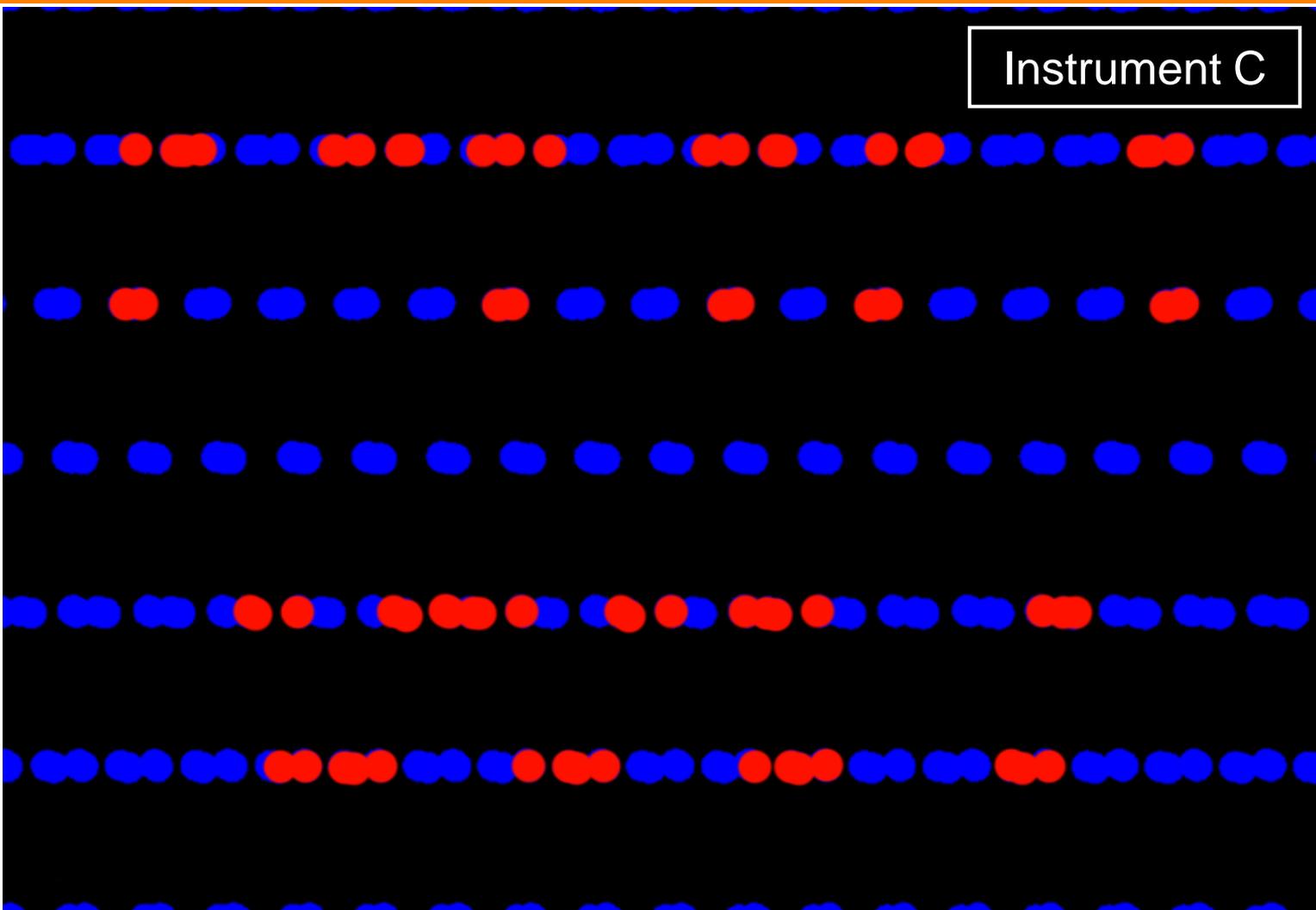




Instrument C

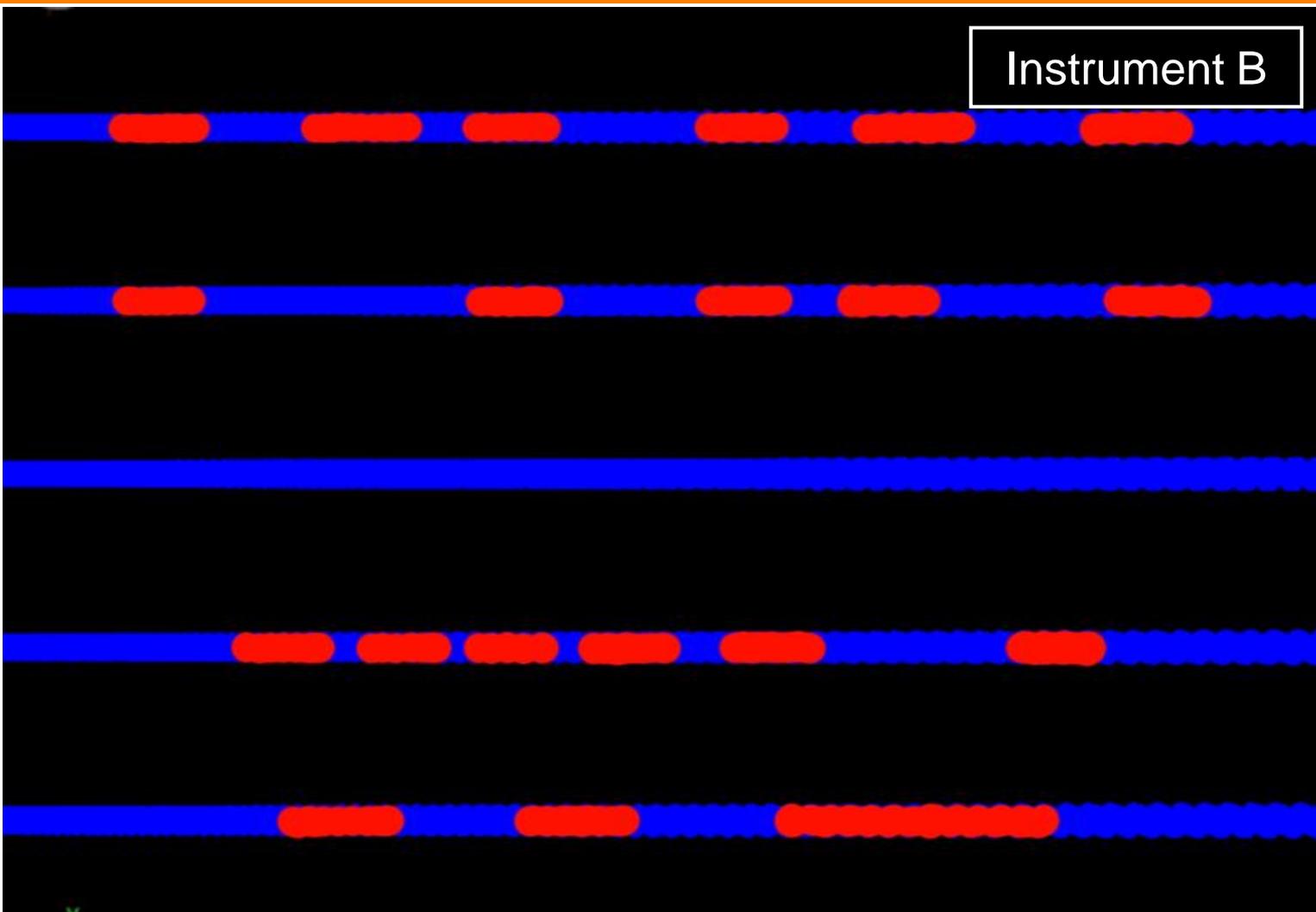
2000 m AGL  
140 kn GSP  
60 deg FOV

mountainous  
terrain  
near edge of  
swath





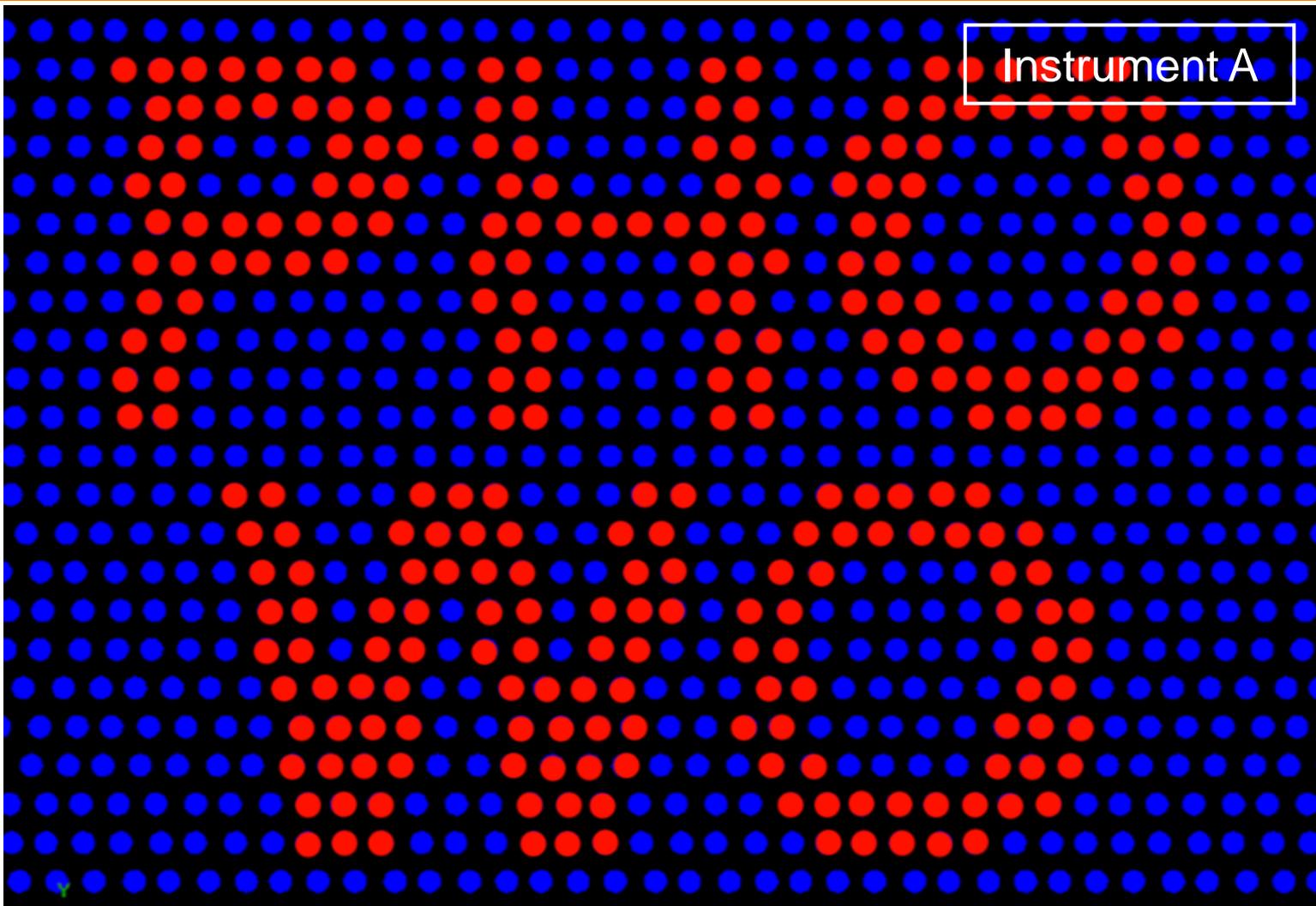
Instrument B



2000 m AGL  
140 kn GSP  
60 deg FOV

mountainous  
terrain  
near edge of  
swath





2000 m AGL  
140 kn GSP  
60 deg FOV

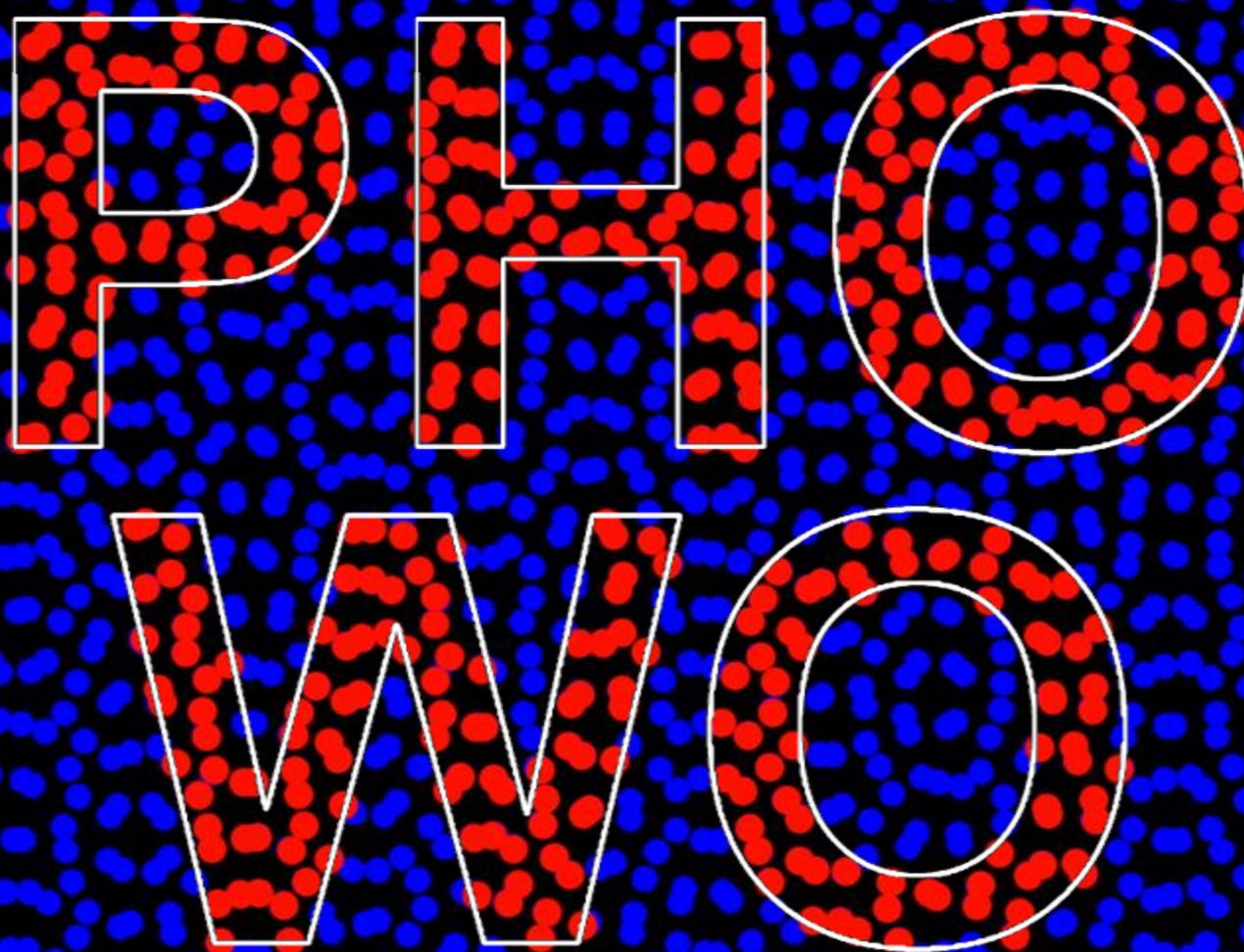
mountainous  
terrain  
near edge of  
swath







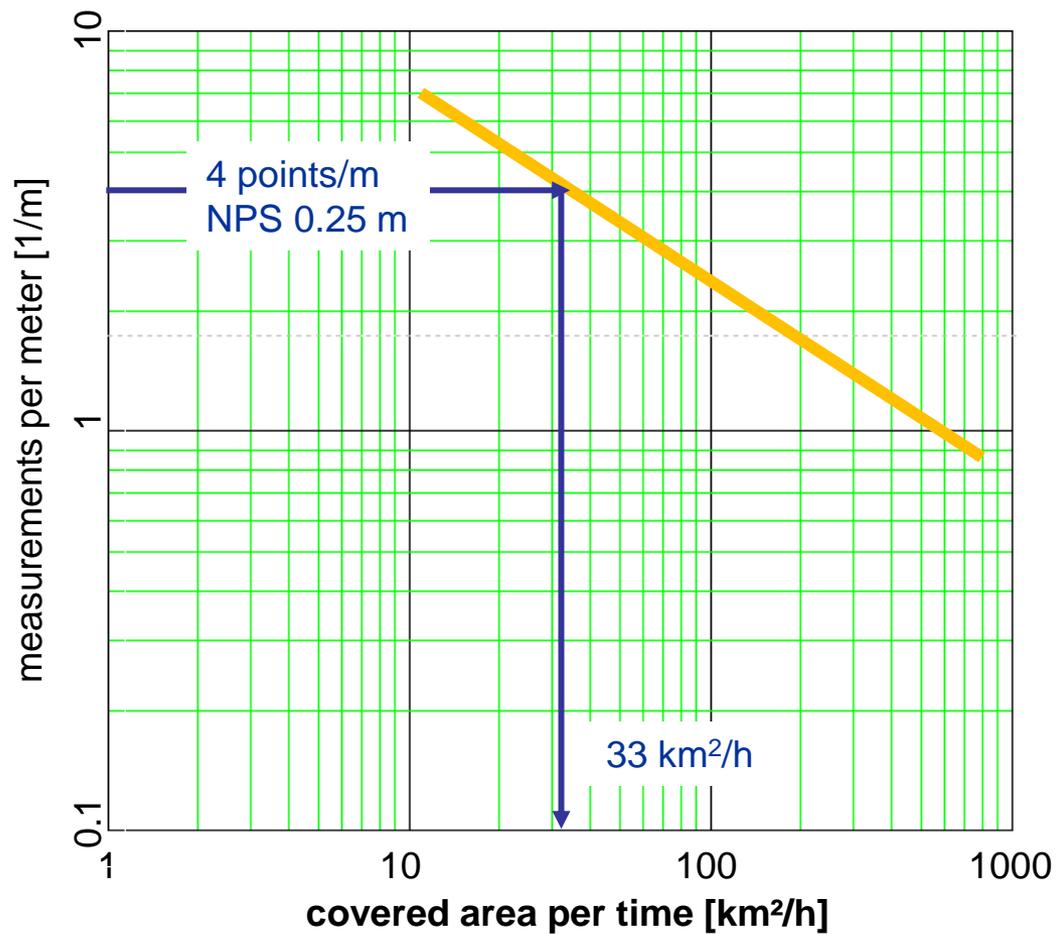
**RIEGL**  
**LMS-Q1560**



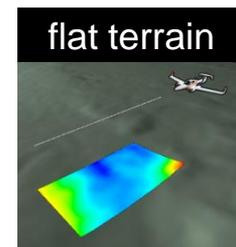
2000 m AGL  
140 kn GSP  
60 deg FOV

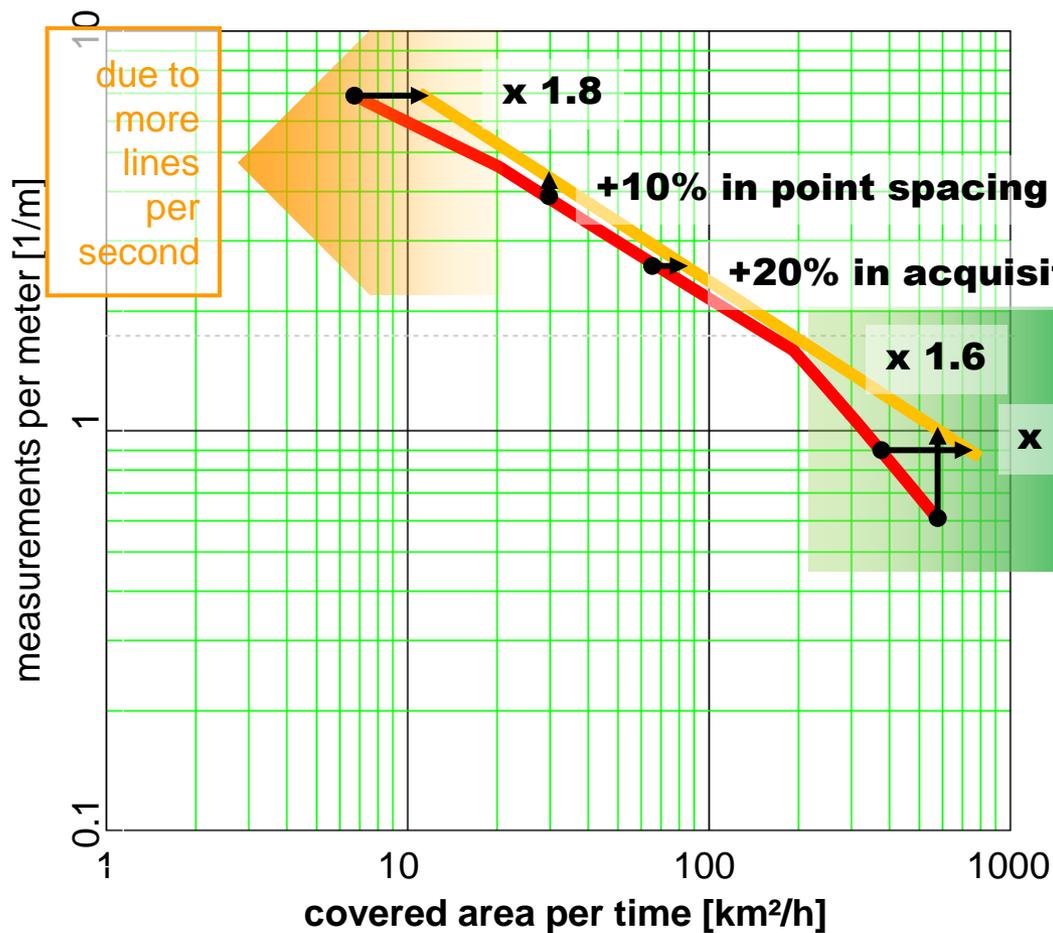
mountainous  
terrain  
near edge of  
swath





— instrument A, **RIEGL LMS-Q780**  
**266 k meas./sec**

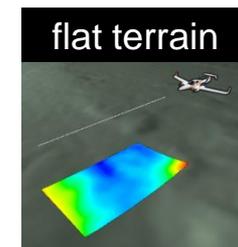


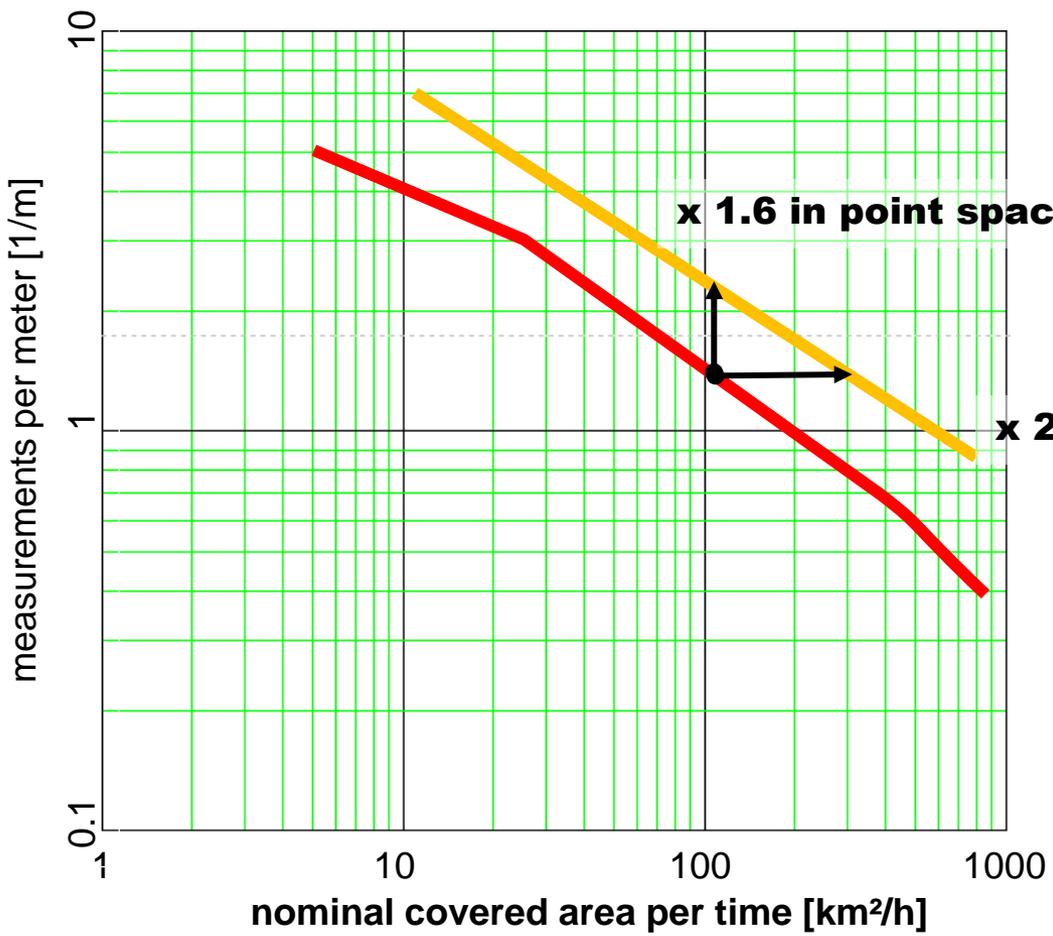


— instrument A, **RIEGL LMS-Q780**  
266 k meas./sec

— instrument B  
500 k meas./sec

more improvement by  
multiple-MTA-zone  
acquisition and processing



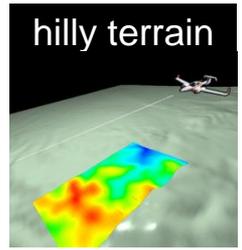


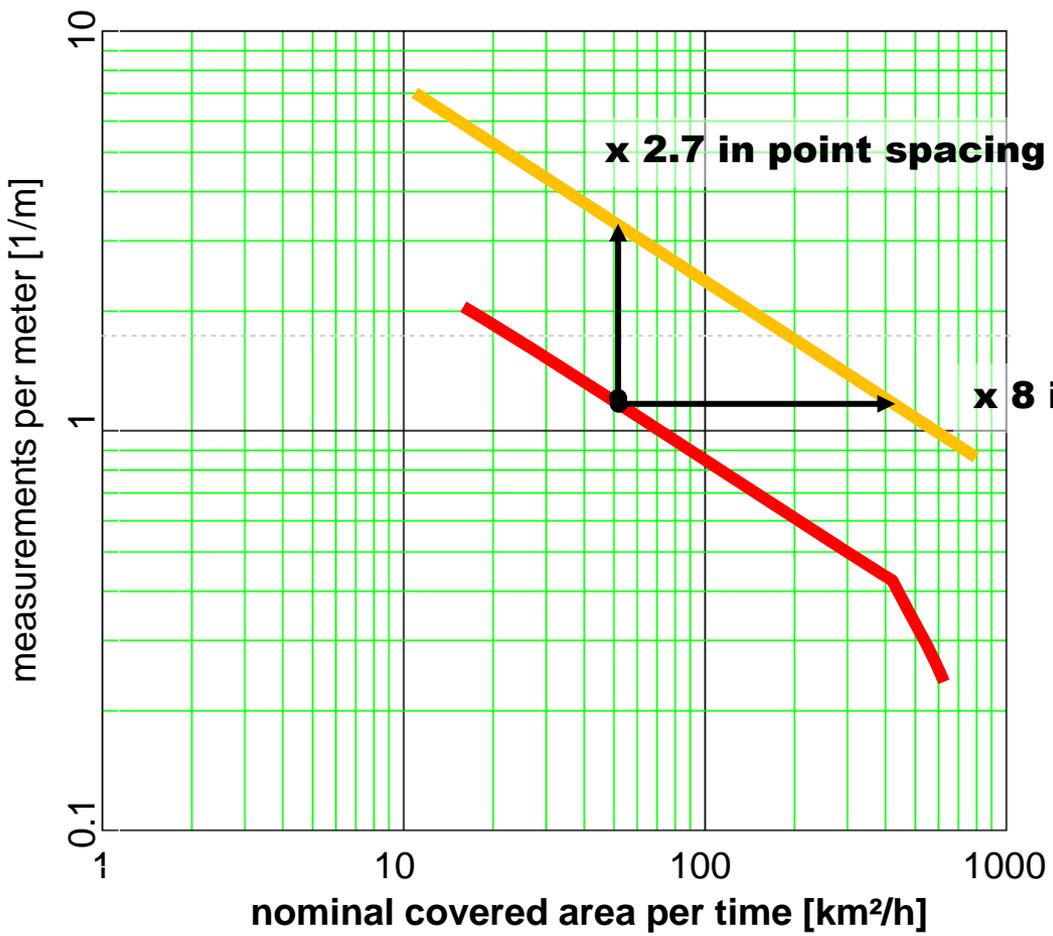
— instrument A, *RIEGL LMS-Q780*  
 266 k meas./sec  
— instrument B  
 up to 500 k meas./sec

**x 1.6 in point spacing**

**x 2.6 in acquisition speed**

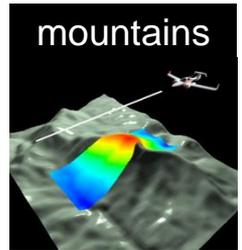
**variation in AMSL  
within strip: 200 m**





- instrument A, *RIEGL LMS-Q780*  
266 k meas./sec
- instrument B  
up to 500 k meas./sec

**variation in AMSL  
within strip: 1000 m**





high ground sampling frequency  
low nominal point spacing

**AND**

high acquisition speed

- fast scan at high FOV (polygon mirror)
- no interference problems (single channel or sophisticated dual channel scanner design)
- wide performance envelope
- high pulse repetition rate at high AGL (high-MTA-zone processing capability)

“it is the point spacing, not the number of measurements on the ground”

